



An Improved RSA based on Double Even Magic Square of order 32

Shahla Uthman Umar-college of science- University of Kirkuk

Shahla_umar@uokirkuk.edu.iq

Shahla_aothman@yahoo.com

[Abstract]

Because of the computers systems discovery and the use of computer networks between countries, security is very important to transfer confidential information over the networks; traditional cryptographic systems such as Rivest-Shamir-Adlemen (RSA) are depend on guesswork as well as mathematics. Information theory illustrates that conventional cryptographic systems cannot be regarded fully secure unless the private key ; which it is used once only ; is at least as long as the plain text. And another limitation is using ASCII value to represent the plaintext, So the repetition of characters in the plain text will appear in the cipher text therefore we have given approach to generate magic square of order 32 which cannot be easily traced and use this square in the cryptography which it is used to improve efficiency through providing an additional level of security to encryption. Through of the characteristics of magic squares, and it's some complex conditions (non-repetition property), these squares generates a huge numbers of non-duplicate random numbers which can be used to represent the numerals rather than ASCII values as well as the magic square is also used to generate the keys for public key encryption algorithms.

[Keywords: Magic Square, RSA, Public Key Cryptosystem, Encryption algorithm, key.]

تحسين خوارزمية التشفير RSA باستخدام المربعات السحرية الفردية

المزدوجة ذات المرتبة ٣٢



شهلة عثمان عمر – كلية العلوم – جامعة كركوك

Shahla_umar@uokirkuk.edu.iq

Shahla_aothman@yahoo.com

المخلص

بسبب اكتشاف أنظمة الحواسيب واستخدام شبكات الحاسوب بين البلدان، فإن أمن البيانات مهم جدا لنقل (تعتمد على التخمين بالإضافة الى RSA المعلومات السرية عبر الشبكات ، واكثر أنظمة التشفير التقليدية مثل) الرياضيات. توضح نظرية المعلومات أن أنظمة التشفير التقليدية لا يمكن اعتبارها آمنة تماما إلا إذا كان المفتاح الخاص والتي يتم استخدامها مرة واحدة فقط على الأقل بطول النص الصريح. ومن القيود الأخرى في هذه الطريقة هو استخدام (لتمثيل النص الصريح، وبالتالي فإن تكرار الأحرف في النص الصريح سوف تظهر في النص المشفر ASCII قيمة) لذلك اقترحنا طريقة جديدة لتوليد المربعات السريعة ذات المرتبة ٣٢ والتي لا يمكن تتبعها والتنبوء بقيمتها بسهولة واستخدام هذه المربعات في التشفير والذي يستخدم لتحسين كفاءة التشفير من خلال توفير مستوى إضافي من الأمان . من خلال خصائص المربعات السحرية، وبعض شروطها المعقدة (مثل خاصية عدم التكرار للقيم)، هذه المربعات تولد (، وكذلك ASCII أعدادا كبيرة من الأرقام العشوائية غير المكررة والتي يمكن استخدامها لتمثيل الأرقام بدلا من القيم) المربعات السحرية تستخدم أيضا لتوليد مفاتيح خوارزميات التشفير بالمفتاح العام.

الكلمات المفتاحية:- المربع السحري، نظام التشفير بالمفتاح العام، خوارزمية التشفير، [

المفتاح

1. Introduction

Cryptography pointed completely on encryption, which is the process of transforming original information ([plaintext](#)) into unreadable text ([cipher text](#)), while

Web Site: www.kujss.com Email: kirkukjournsci@yahoo.com,
kirkukjournsci@gmail.com



decryption is the inverse, Converting from the unreadable cipher text back to plaintext. In cipher, there are two algorithms, the encryption and the reversing decryption [1].

There are two kinds of cryptosystems, [symmetric](#) and [asymmetric](#). In asymmetric systems there are two keys, the first one (public key) is used to encrypt a message while the second one (private key) is used to decrypt it, therefore these systems increase the security of communication [1]. An example of asymmetric systems is RSA, The security of several cryptographic systems relates with the creation of unexpected elements like the secret key in the DES algorithms, the key stream in the one-time pad and the prime P, and Q in the RSA encryption. In every these instances, the keys made must be sufficient in size and the arbitrary. However, RSA is not completely secure or secure against chosen cipher text attacks. If all variables are selected in such a way that it's impossible to compute the private key (d) from the public key (n, e), or choosing P, Q are incredibly large. Even if the above variables were selected carefully, none of the computational problems are completely guaranteed enough [2]. To encrypt the clear message characters, their ASCII values are taken which is possible that the same cipher text is produced for the characters which occur in several positions in the plaintext. To eliminate this problem, this paper attempts to improve a method with "doubly even magic squares (DEMS)" of order 32 (32×32) which equals to 1024 different values and dividing this magic square to different corresponding ASCII tables (each table is 128 ASCII characters). Thus, instead of taking the ASCII values of the characters to encrypt, different numerals representing the location of ASCII values in the magic square are taken and also using the same magic square to select two prime numbers (P and Q) which is used to generate the public key (e, n) then these numerals are encrypted using "RSA cryptosystem".

2. Related Work



As the intruder has the chance of finding the public key value (e), then finding the decryption key (d) value directly and decrypts the cipher text, "Amare Anagaw Aycle and Vuda Sreenivasarao" [3] suggested an efficient representation of RSA algorithm by applying mathematical logics on two public keys rather than sending the public key (e) in RAS algorithm.. While "Gopinath Ganapathy and K Mani" [4] suggested a new layar of security to public key algorithm by providing more security to the cryptosystem using magic squares idea. In July 2012 Sonia Goyat[5] proposed a new algorithm by applying the genetic algorithm to cryptography and alter the algorithm to generate more powerful keys and also the random values, which it is used to generate keys, are unique. Then A new algorithm "Modified Subset-Sum cryptosystem over RSA" was presented by Sonal Sharma, Saroj Hiranwal, Prashant Sharma[6] which it is secured against Shamir attacks on RSA as well as various sorts of Mathematical attacks. And in January of the same year Prasant Sharma, Amit Kumar Gupta et al [7] studied the rapidity of RSA public key cryptosystem to decline the time taken for finding factor for a huge number. They suggested a new algorithm and its output was compared with "Fermats factorization Algorithm and trial division algorithm".

3. Proposed Methodology

The Improved RSA based on Double Even Magic Square (DEMS) is:-

Step 1:- Generate Doubly Even Magic Square of order 32 (32×32) which contains totally 1024 values and divide it to eight different quadrants each consists of 128 characters. Each different quadrant corresponds to one ASCII set (128 characters).

Step 2:- For every letter in the plain text, the numerals corresponding to its position in different quadrants of magic square are taken then these numerals are encrypted and decrypted using RSA public key cryptosystem.



Step 3:-Use the same magic square to select two prime numbers P and Q which is used to find the public key in RSA, from the range (1-1024) two numbers are selected randomly and then from this limit any two prime number (p and q) are selected which cannot be trace because of their randomness. (figure 1)

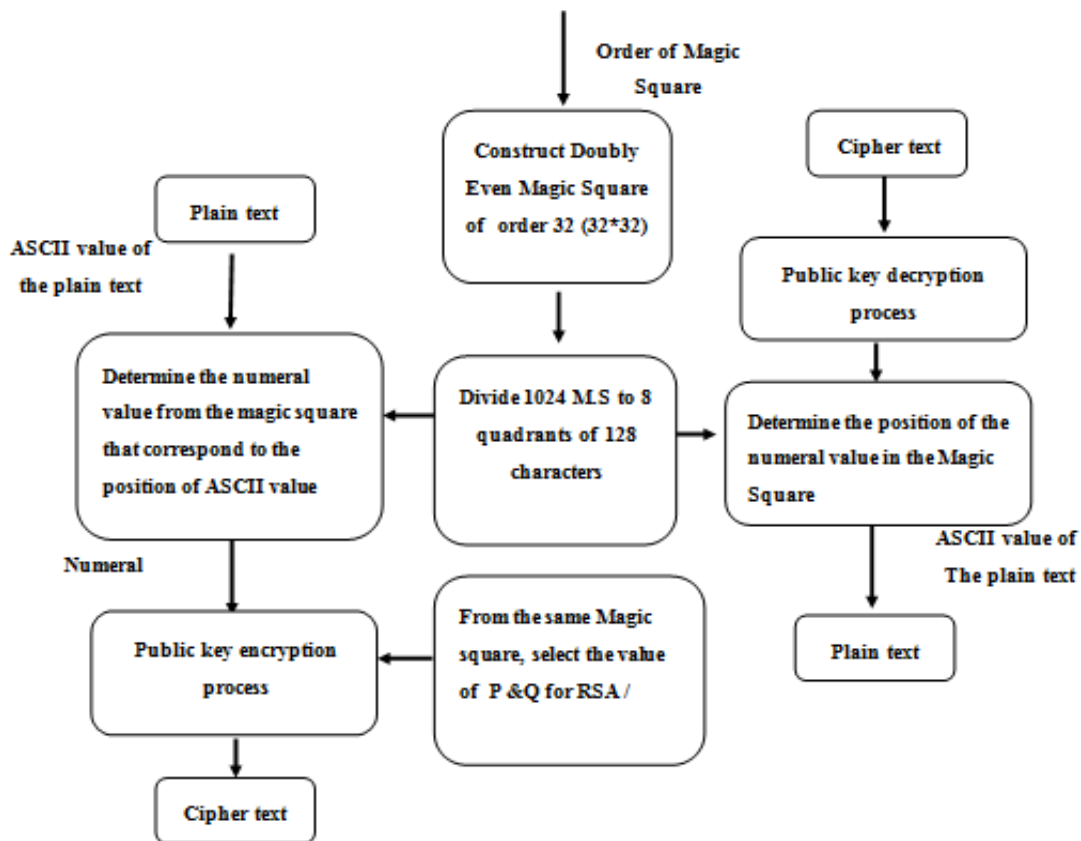


Figure 1: The Proposed Security Model

3.1. Construction of Magic Square



"A magic square" of order n is a square array or an array of n^2 numbers which fulfils the condition that the sum of the elements of each row and column, as well as the main diagonals, is the same number which it is called the magic. Generally, the entries are thought of as the natural numbers $1, 2, \dots, n^2$, where each number is used exactly once. Magic Squares utilized to generate a huge number of random keys. The number of magic squares of order 4 (4x4) using the numbers from 1 to 16 and magic constant (34) is 880 magic square, magic squares of order 6 (6x6) or above require a huge amount of calculations where normal computer cannot be resolved, according to some estimates the number exceeds (1.7745×10^{19}) through rotate rows and columns. The use of magic squares in data encryption gives more security because of the difficulty of magic squares analysis using frequency analysis, Or by using the principle of guesswork and the trial and error to decode the text [8]. "The magic constants for normal magic squares of orders $n = 3, 4, 5, 6, 7, 8 \dots$ are 15, 34, 65, 111, 175, 265... respectively".

$$\text{Sum} = n(n^2+1)/2$$

Magic squares are classified into three types: odd, doubly even and singly even [9]

3.2. Construction of Doubly Even Magic Squares

A doubly even magic square is a square matrix of order n , where n is divisible by four only, while a singly even magic square is a square matrix of order n , where n is even but not divisible by four. [9]

"A (4x4) magic square is a doubly even magic square, and one of the three types of magic square. The other two types are":

- odd (where $n=3, 5, 7, 9, 11, \dots$)



- singly even (even but *not* a multiple of 4 where $n=6, 10, 14, 18, 22,$ etc.) [4][10].

In this paper we focused only on the implementation of doubly even magic square of order 32 (32×32) and their affect to enhance the public-key cryptosystem (RSA), to construct "doubly even magic squares", starting with the simplest (8×8). In 8 by 8 grids, in first step we write the numbers 1 through 64 from left to right (figure 2.a). Then "flip" the numbers in the diagonals (the red lines). That is to say, exchange 64 & 1, 55 & 10,....., and 57 & 8 and 50 & 15 and so on, and we will have a magic square constant= 260 (figure 2.b)._ in the second step we divide 8 by 8 square into 4 blocks (each block is 4 by 4) then replace and flip the elements in the secondary diagnose of block 1 with the elements in the secondary diagnose of block 4(gray cells) and replace and flip the elements in the main diagnose of block 2 with the elements in the main diagnose of block 3(yellow cells)(figure 2.c)

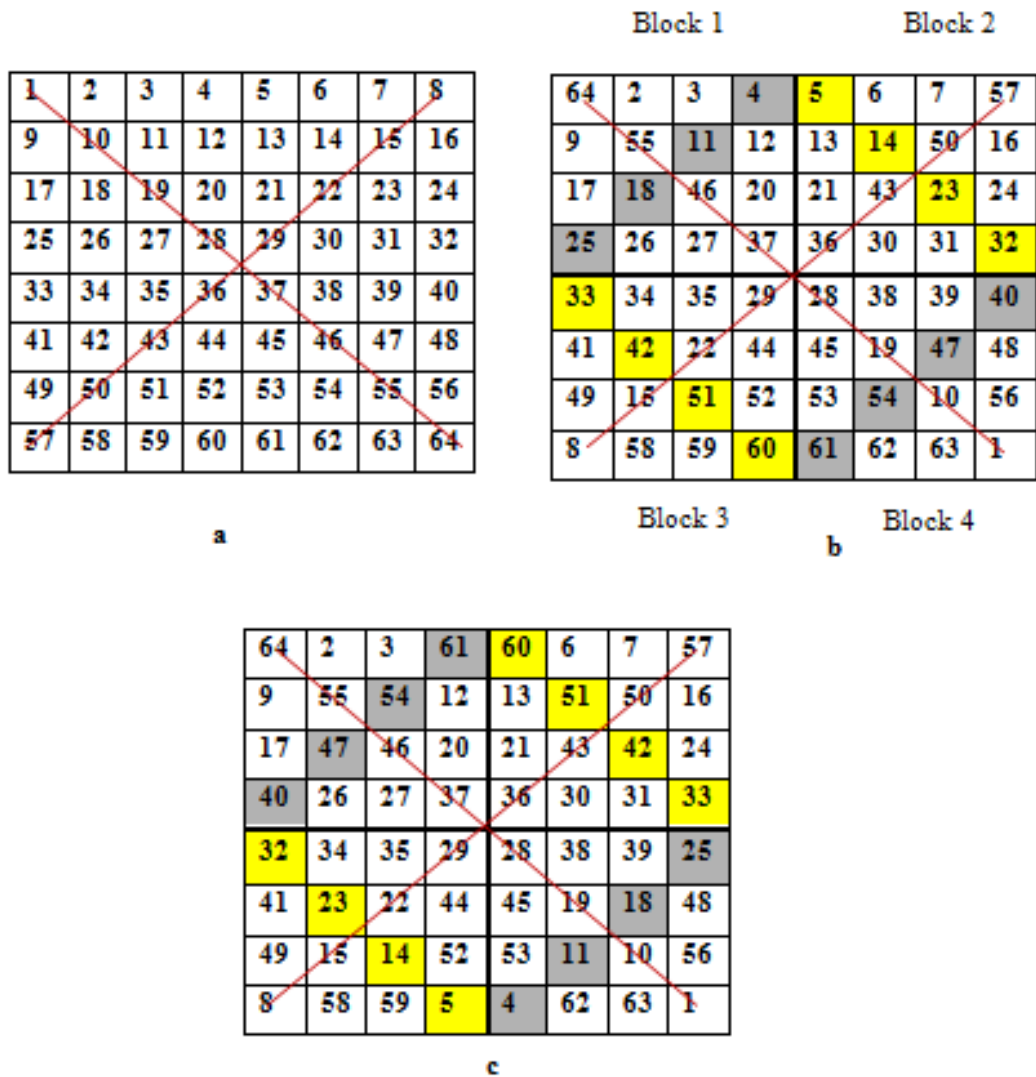


Figure 2 : Doubly Even Magic Square 8 by 8(constant 260)

With the same approach we construct a doubly even magic square of order 32 (Figure 3)



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1024	2	3	1021	1020	6	7	1017	1016	10	11	1013	1012	14	15	1009	1008	18	19	1005	1004	22	23	
1001	1000	26	27	997	996	30	31	993															
33	991	990	36	37	987	986	40	41	983	982	44	45	979	978	48	49	975	974	52	53	971	970	
56	57	967	966	60	61	963	962	64															
65	959	958	68	69	955	954	72	73	951	950	76	77	947	946	80	81	943	942	84	85	939	938	
88	89	935	934	92	93	931	930	96															
928	98	99	925	924	102	103	921	920	106	107	917	916	110	111	913	912	114	115	909	908	118	119	
905	904	122	123	901	900	126	127	897															
896	130	131	893	892	134	135	889	888	138	139	885	884	142	143	881	880	146	147	877	876	150	151	
873	872	154	155	869	868	158	159	865															
161	863	862	164	165	859	858	168	169	855	854	172	173	851	850	176	177	847	846	180	181	843	842	
184	185	839	838	188	189	835	834	192															
193	831	830	196	197	827	826	200	201	823	822	204	205	819	818	208	209	815	814	212	213	811	810	
216	217	807	806	220	221	803	802	224															
800	226	227	797	796	230	231	793	792	234	235	789	788	238	239	785	784	242	243	781	780	246	247	
777	776	250	251	773	772	254	255	769															
768	258	259	765	764	262	263	761	760	266	267	757	756	270	271	753	752	274	275	749	748	278	279	
745	744	282	283	741	740	286	287	737															
289	735	734	292	293	731	730	296	297	727	726	300	301	723	722	304	305	719	718	308	309	715	714	
312	313	711	710	316	317	707	706	320															
321	703	702	324	325	699	698	328	329	695	694	332	333	691	690	336	337	687	686	340	341	683	682	
344	345	679	678	348	349	675	674	352															
672	354	355	669	668	358	359	665	664	362	363	661	660	366	367	657	656	370	371	653	652	374	375	
649	648	378	379	645	644	382	383	641															
640	386	387	637	636	390	391	633	632	394	395	629	628	398	399	625	624	402	403	621	620	406	407	
617	616	410	411	613	612	414	415	609															
417	607	606	420	421	603	602	424	425	599	598	428	429	595	594	432	433	591	590	436	437	587	586	
440	441	583	582	444	445	579	578	448															
449	575	574	452	453	571	570	456	457	567	566	460	461	563	562	464	465	559	558	468	469	555	554	
472	473	551	550	476	477	547	546	480															
544	482	483	541	540	486	487	537	536	490	491	533	532	494	495	529	528	498	499	525	524	502	503	
521	520	506	507	517	516	510	511	513															
512	514	515	509	508	518	519	505	504	522	523	501	500	526	527	497	496	530	531	493	492	534	535	
489	488	538	539	485	484	542	543	481															
545	479	478	548	549	475	474	552	553	471	470	556	557	467	466	560	561	463	462	564	565	459	458	
568	569	455	454	572	573	451	450	576															
577	447	446	580	581	443	442	584	585	439	438	588	589	435	434	592	593	431	430	596	597	427	426	
600	601	423	422	604	605	419	418	608															
416	610	611	413	412	614	615	409	408	618	619	405	404	622	623	401	400	626	627	397	396	630	631	
393	392	634	635	389	388	638	639	385															
384	642	643	381	380	646	647	377	376	650	651	373	372	654	655	369	368	658	659	365	364	662	663	
361	360	666	667	357	356	670	671	353															



673	351	350	676	677	347	346	680	681	343	342	684	685	339	338	688	689	335	334	692	693	331	330
696	697	327	326	700	701	323	322	704														
705	319	318	708	709	315	314	712	713	311	310	716	717	307	306	720	721	303	302	724	725	299	298
728	729	295	294	732	733	291	290	736														
288	738	739	285	284	742	743	281	280	746	747	277	276	750	751	273	272	754	755	269	268	758	759
265	264	762	763	261	260	766	767	257														
256	770	771	253	252	774	775	249	248	778	779	245	244	782	783	241	240	786	787	237	236	790	791
233	232	794	795	229	228	798	799	225														
801	223	222	804	805	219	218	808	809	215	214	812	813	211	210	816	817	207	206	820	821	203	202
824	825	199	198	828	829	195	194	832														
833	191	190	836	837	187	186	840	841	183	182	844	845	179	178	848	849	175	174	852	853	171	170
856	857	167	166	860	861	163	162	864														
160	866	867	157	156	870	871	153	152	874	875	149	148	878	879	145	144	882	883	141	140	886	887
137	136	890	891	133	132	894	895	129														
128	898	899	125	124	902	903	121	120	906	907	117	116	910	911	113	112	914	915	109	108	918	919
105	104	922	923	101	100	926	927	97														
929	95	94	932	933	91	90	936	937	87	86	940	941	83	82	944	945	79	78	948	949	75	74
952	953	71	70	956	957	67	66	960														
961	63	62	964	965	59	58	968	969	55	54	972	973	51	50	976	977	47	46	980	981	43	42
984	985	39	38	988	989	35	34	992														
32	994	995	29	28	998	999	25	24	1002	1003	21	20	1006	1007	17	16	1010	1011	13	12	1014	1015
9	8	1018	1019	5	4	1022	1023	1														

Figure 3: Doubly Even Magic Square of order 32

3.2. Algorithm of generating of Doubly Even magic square:



Input: n is the order of doubly even magic square.

Output: Doubly Even Magic Square matrix[n][n] of order 32.

Set the array $x[n][n]$ equal to 0

Set the array $y[n][n]$ equal to 0

Set $index$ to 1

For $i=1$ to n

 For $j=1$ to n

 Set $tmp = ((i + 1) \bmod 4) / 2$;

 Set $x[i][j]$ to tmp

 Set $y[i][j]$ to tmp

 Set $Matrix[i][j] = index$

 Set $index$ to $index+1$

 End for j

End for i

For $i=1$ to n

 For $j=1$ to n

 If $x[i][j] = y[i][j]$ then

 Set $matrix[i][j] = n * n + 1 - matrix[i][j]$;

 End if

 End for j

End for i

4. Experiments and Results



1. Magic Square of order 4 is first generated using the proposed algorithm which satisfies the double even magic squares requirements with magic constant (34) (figure):-

16	2	3	13
5	11	10	8
9	7	6	12
4	14	15	1

Figure 3: Double even magic square of order 4

2. with the same way, we construct magic square of order 8, 16, 32 with magic constant 260, 2056, 16400 respectively (figure 4) (figure 5)(magic square of order 32 shown in figure 3) :-

64	2	3	61	60	6	7	57
9	55	54	12	13	51	50	16
17	47	46	20	21	43	42	24
40	26	27	37	36	30	31	33
32	34	35	29	28	38	39	25
41	23	22	44	45	19	18	48
56	10	11	53	52	14	15	49
8	58	59	5	4	62	63	1

Figure 4: Double even magic square of order 8



256	2	3	253	252	6	7	249	248	10	11	245	244	14	15	241
17	239	238	20	21	235	234	24	25	231	230	28	29	227	226	32
33	223	222	36	37	219	218	40	41	215	214	44	45	211	210	48
208	50	51	205	204	54	55	201	200	58	59	197	196	62	63	193
192	66	67	189	188	70	71	185	184	74	75	181	180	78	79	177
81	175	174	84	85	171	170	88	89	167	166	92	93	163	162	96
97	159	158	100	101	155	154	104	105	151	150	108	109	147	146	112
144	114	115	141	140	118	119	137	136	122	123	133	132	126	127	129
128	130	131	125	124	134	135	121	120	138	139	117	116	142	143	113
145	111	110	148	149	107	106	152	153	103	102	156	157	99	98	160
161	95	94	164	165	91	90	168	169	87	86	172	173	83	82	176
80	178	179	77	76	182	183	73	72	186	187	69	68	190	191	65
64	194	195	61	60	198	199	57	56	202	203	53	52	206	207	49
209	47	46	212	213	43	42	216	217	39	38	220	221	35	34	224
225	31	30	228	229	27	26	232	233	23	22	236	237	19	18	240
16	242	243	13	12	246	247	9	8	250	251	5	4	254	255	1

Figure 5: Double even magic square of order 16



It is so difficult to determine the number of unique magic squares of different orders, but the number of unique magic squares of order $n=1, 2, \dots$ are 1, 0, 1, 880, 275305224 . The 880 squares of order 4 were enumerated by "Frénicle de Bessy" in 1693, and are illustrated in Berlekamp (1982). "R. Schroepel" in 1973 calculate the number of (5×5) magic squares[13], while the number of (6×6) squares is not identified, but "Pinn and Wiczerkowski (1998)" estimated it to be $(1.7745(16) \times 10^{19})$ [14].

5. Example on RSA with double even Magic Square

RSA is implemented to illustrate the effect of using magic squares to enhance the security of public key encryption schemes. The secret key in the system consists of two prime numbers (P and Q) and an exponent (d) while the public key consists of the modulus $N = P \cdot Q$ and an exponent (e) where $d = e^{-1} \pmod{(P-1)(Q-1)}$. The user calculates $C = M^e \pmod{n}$ for encryption and $M = C^d \pmod{n}$ is done for decryption (for any message [11],[12]).

In this paper, the modulus of N, M, and C should have a length of 512-1024 bits in order to prevent the known attacks. Using the above algorithm, we construct a "doubly even magic square" of order 32 which contains 1024 different (non repetition) values, as the characters set consists of 128 ASCII values, the magic square is divided logically into different 8 matrices each one with 128 values corresponding to individual ASCII character, for getting more realization of the proposed matter, we take an example, assume $P=13$, $Q=17$ and the public key (e) =11, then $N=221$, and $(P-1) \cdot (Q-1)=192$.now the secret key(d) = 35 . To encrypt the message (A CAR), the ASCII values of A, C and R are 65, 67 and 82 respectively, so to encrypt A which appears in first and third position in the plain text, the numerals which appear at 65th position of first matrices and at 65th position of third matrices(figure 3 which is divided logically into 8 matrice) are taken respectively, Thus $N_p(A)=959$ and 831, $N_p(C)=68$ and $N_p(R) =942$. And the cipher $C(A)=959^{11} \pmod{221}=82$, $C(C)=68^{11} \pmod{221}=204$, $C(A)=831^{11} \pmod{221}=77$, $C(R)=942^{11} \pmod{221}=167$ similarly we use this



substitution for every repeated character in the plaintext, therefore for each repeated character A, B, C,...(which appears more than once in the plain text), different cipher texts are generated.

6. The comparison between ordinary RSA algorithm and proposed RSA with Double Even Magic Square:-

To illustrate the result of RSA algorithm with magic square, the plain text (MESSAGE) is first encrypted using existing RSA(if $p=19$, $q=23$, $n=437$, $(p-1).(q-1)=396$, $e=13$ then $d=61$) and the output is shown in table 1. It is clear that the characters (E and S) appear twice in the plaintext, therefore in the ordinary RSA, the cipher text of them is the same (425), while in the suggested (RSA with DEMS), the cipher text value of the first (E) which it is (397) is differ from the second (E) which it is (298) and the same thing with any repeated characters in the plaintext, This methodology is implemented in C#

Table 1. Comparison of cipher text

Ordinary RSA			RSA with Double even magic square		
Plain text	ASCII value	Cipher text	Plain text	MS value	Cipher text
M	77	248	M	947	62
E	69	69	E	955	397
S	83	425	S	84	350
S	83	425	S	212	90
A	65	122	A	959	348
G	71	211	G	72	124
E	69	69	E	827	298



7. Conclusion

This work prevents any hacker from getting the plain text in a readable form even if they obtained the keys because of using the numerical values of magic square rather than the ASCII values of characters (rather than of unique ASCII table, 8 tables with various set of values are used). It is unsolved problem to determine the number of magic squares of order 32 which is used in this paper. The security aspect of RSA is improved because there are no duplicated values in Magic Squares. In the ordinary RSA, the same cipher text values are generated whenever the same characters are repeated in the plain text, while in the proposed (RSA with DEMS) different values are produced in the cipher text for each occurrence of the same character in the plain text. It plays an important role in increasing the randomness and security of the algorithm. One of the issues in the proposed work is additional time needed for the construction of Magic squares initially.

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Web Site: www.kujss.com Email: kirkukjournsci@yahoo.com,
kirkukjournsci@gmail.com



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