

17 New Existences linear $[n,3,d]_{19}$ Codes by Geometric Structure Method in $PG(2,19)$

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الملخص

الهدف من هذا البحث هو إثبات وجود 17 شفرة خطية جديدة , $[337,3,318]_{19}$, $[289,3,271]_{19}$, $[266,3,249]_{19}$, $[246,3,230]_{19}$, $[219,3,204]_{19}$, $[206,3,192]_{19}$, $[181,3,168]_{19}$, $[157,3,145]_{19}$, $[141,3,130]_{19}$, $[120,3,110]_{19}$, $[112,3,103]_{19}$, $[82,3,74]_{19}$, $[72,3,65]_{19}$, $[54,3,48]_{19}$, $[37,3,32]_{19}$, $[26,3,22]_{19}$, $[13,3,10]_{19}$ بواسطة طريقة البناء (التركيب) الهندسي في المستوي الإسقاطي $PG(2,19)$.

ABSTRACT

The purpose of this paper is to prove the existence of 17 new linear $[337,3,318]_{19}$, $[289,3,271]_{19}$, $[266,3,249]_{19}$, $[246,3,230]_{19}$, $[219,3,204]_{19}$, $[206,3,192]_{19}$, $[181,3,168]_{19}$, $[157,3,145]_{19}$, $[141,3,130]_{19}$, $[120,3,110]_{19}$, $[112,3,103]_{19}$, $[82,3,74]_{19}$, $[72,3,65]_{19}$, $[54,3,48]_{19}$, $[37,3,32]_{19}$, $[26,3,22]_{19}$, $[13,3,10]_{19}$ codes by geometric structure method in $PG(2,19)$.

Keywords: Linear code , $[n,k,d]_q$ codes, Finite geometry, (k,r) -arc.

1. Introduction [1]

Let $GF(q)$ denote the Galois field of q elements and $V(3,q)$ be the vector space of row vectors of length three with entries in $GF(q)$. Let $PG(2,q)$ be the corresponding projective plane. The points of $PG(2,q)$ are the non-zero vectors of $V(3,q)$ with the rule that $X=(x_1,x_2,x_3)$ and $Y=(\delta x_1, \delta x_2, \delta x_3)$ represent the same point, where $\delta \in GF(q) \setminus \{0\}$. The number of points of $PG(2,q)$ is q^2+q+1 . If the point $P(X)$ is the equivalence class of the vector X , then we will say that X is a vector representing $P(X)$. A subspace of dimension one is a set of points all of whose representing vectors form a subspace of dimension two of $V(3,q)$. Such subspaces are called lines. The number of lines in $PG(2,q)$ is q^2+q+1 . There are $q+1$ points on every line and $q+1$ lines through every point.

1.1 Definition " Double Blocking set " [5]

A double blocking set in a projective plane $PG(2,q)$ is a set S of points with the property that every line contains at least two points of S .

1.2 Definition " A (k,r) -arc " [2]

A (k,r) -arc K in $PG(2,q)$ is a set of k points with condition no line of the plane contains more than k points and there exists at least one line of the plane

which contains k points. A (k,r) -arc is called complete arc if it is not contained in a $(k+1,r)$ -arc.

1.3 Definition " The Linear $[n,k,d]_q$ codes " [4]

The linear codes $[n,k,d]_q$ in $PG(2,q)$ where n is the length of codes and k is the dimension of codes, and minimum Hamming distance between the codes is called d over the Galois field $GF(q)$.

1.4 Definition " i -secant " [1]

A line L in $PG(2,q)$ is an i -secant of a (k,r) -arc if $|L \cap K|=i$

1.5 Theorem 1: [4]

There exists linear $[n,3,d]_q$ codes if and only if there exists an $(n,n-d)$ -arc in $PG(2,q)$

2. The geometrical structure method in $PG(2,19)$.

Let $A=(1,2,21,41)$ be the set of reference unit and reference points in $PG(2,13)$ where $1=(1,0,0)$, $2=(0,1,0)$, $21=(0,0,1)$, $41=(1,1,1)$

A is $(4,2)$ -arc, since no three points of A are collinear,

$[1,2]=[1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20]$

$[1,21]=[1,21,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39]$

$[1,41]=[1,40,41,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58]$

$[2,21]=[2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,287,306,325,344,363]$

$[2,41]=[2,22,41,60,79,98,117,136,155,174,193,212,231,250,269,288,307,326,345,364]$

$[21,41]=[3,21,41,61,81,101,121,141,161,181,201,221,241,261,281,301,321,341,361,381]$

The diagonal points of A are the points $\{3,22,40\}$ where, $L_1 \cap L_6 = 3$; $L_2 \cap L_5 = 22$; $L_3 \cap L_4 = 40$.

There are one hundred and one points of index zero for A , which are:

62,63,64,65,66,67,68,69,70,71,72,73,74,75,76,77,80,82,83,84,85,86,87,88,89,90,91,92,93,94,95,96,99,100,102,103,104,105,106,107,108,109,110,111,112,113,114,115,118,119,120,122,123,124,125,126,127,128,129,130,131,132,133,134,157,138,139,140,142,143,144,145,146,147,148,149,150,151,152,153,156,157,158,159,160,162,163,164,165,166,167,168,169,170,171,172,175,176,177,178,179,180,182,183,184,185,186,187,188,189,190,191,194,195,196,197,198,199,200,202,203,204,205,206,207,208,209,210,213,214,215,216,217,218,219,220,222,223,224,225,226,227,228,229,232,233,234,235,236,237,238,239,240,242,243,244,245,246,247,248,251,252,253,254,255,256,257,258,259,260,262,263,264,265,266,267,270,271,271,273,274,275,276,277,278,279,280,282,283,284,285,286,289,290,291,292,293,294,295,296,297,298,299,300,302,303,304,305,308,309,310,311,312,313,314,315,316,317,318,319,320,322,323,324,327,328,329,330,331,332,333,334,335,336,337,338,339,340,342,343,346,347,348,349,350,351,352,353,354,355,356,357,358,359,360,362,365,366,367,368,369,370,371,372,373,374,375,376,377,378,379,380

Hence, A is incomplete $(4,2)$ -arc.

3. The Conics in $PG(2,19)$ Through the Reference and Unit Points

The general equation of the conic is :

$$a_1x^2_1 + a_2x^2_2 + a_3x^2_3 + a_4x_1x_2 + a_5x_1x_3 + a_6x_2x_3 = 0 \dots (1)$$

By substituting the points of the arc A in (1), then:

$1 = (1,0,0)$ implies that $a_1 = 0$, $2 = (0,1,0)$, then $a_2 = 0$, $21 = (0,0,1)$, then

$a_3 = 0, 41 = (1,1,1)$, then

$$a_1 = a_2 = a_3 = 0$$

$$a_4 + a_5 + a_6 = 0.$$

Hence, from equation (1)

$$a_4 x_1 x_2 + a_5 x_1 x_3 + a_6 x_2 x_3 = 0 \dots (2)$$

If $a_4 = 0$, then the conic is degenerated, therefore for $a_4 \neq 0$, similarly $a_5 \neq 0$

and $a_6 \neq 0$,

Dividing equation (2) by a_4 , one can get:

$$x_1 x_2 + \alpha x_1 x_3 + \beta x_2 x_3 = 0$$

$$\text{where } \alpha = a_5/a_4, \beta = a_6/a_4$$

then $\beta = -(1 + \alpha)$, since $1 + \alpha + \beta = 0 \pmod{13}$.

where $\alpha \neq 0$ and $\alpha \neq 12$, for if $\alpha = 0$ or $\alpha = 12$, then degenerated conics, thus $\alpha = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17$ and can be written (2) as :

$$x_1 x_2 + \alpha x_1 x_3 - (1 + \alpha) x_2 x_3 = 0 \dots (3)$$

The equation and the points of the conics of PG(2,19) through the reference and unit points

1. If $\alpha = 1$, then the equation of the conic

$$C_1 = x_1 x_2 + x_1 x_3 + 17 x_2 x_3 = 0,$$

the points of C_1 :

{1,2,21,41,73,89,110,124,153,170,179,209,218,235,264,278,299,315,328,348} which is a complete (20,2)-arc, since there are no points of index zero.

2. If $\alpha = 2$, then the equation of the conic $C_2 = x_1 x_2 + 2x_1 x_3 + 16x_2 x_3 = 0$,

the points of C_2 :

{1,2,21,41,70,95,99,129,142,169,183,210,223,234,257,282,292,312,334,379}, which is a complete (20,2)-arc, since there are no points of index zero .

3. If $\alpha = 3$, then the equation of the conic $C_3 = x_1 x_2 + 3x_1 x_3 + 15x_2 x_3 = 0$,

the points of C_3 :

{1,2,21,41,72,80,102,128,144,172,188,195,217,244,256,276,297,322,355,380}, which is a complete (20,2)-arc, since there are no points of index zero.

4. If $\alpha = 4$, then the equation of the conic $C_4 = x_1 x_2 + 4x_1 x_3 + 14x_2 x_3 = 0$,

the points of C_4 :

{1,2,21,41,67,91,109,123,138,171,189,194,220,240,267,283,293,329,358,374}, which is a complete (20,2)-arc, since there are no points of index zero.

5. If $\alpha = 5$, then the equation of the conic $C_5 = x_1 x_2 + 5x_1 x_3 + 13x_2 x_3 = 0$,

the points of C_5 :

{1,2,21,41,77,85,106,119,140,167,184,204,215,246,251,285,320,335,359,371}, which is a complete (20,2)-arc, since there are no points of index zero.

6. If $\alpha = 6$, then the equation of the conic $C_6 = x_1 x_2 + 6x_1 x_3 + 12x_2 x_3 = 0$,

the points of C_6 :

{1,2,21,41,75,93,115,133,148,168,177,200,213,239,260,290,311,337,350,373}, which is a complete (20,2)-arc, since there are no points of index zero.

7. If $\alpha = 7$, then the equation of the conic $C_7 = x_1 x_2 + 7x_1 x_3 + 11x_2 x_3 = 0$,

the points of C_7 :

{1,2,21,41,65,88,112,132,146,158,176,206,228,237,277,305,308,338,356,368}, which is a complete (20,2)-arc, since there are no points of index zero.

8. If $\alpha = 8$, then the equation of the conic $C_8 = x_1 x_2 + 8x_1 x_3 + 10x_2 x_3 = 0$,

the points of C_8 :

{1,2,21,41,76,96,100,118,147,162,187,199,216,262,279,291,316,331,360,378}, which is a complete (20,2)-arc, since there are no points of index zero.

9. If $\alpha = 9$, then the equation of the conic $C_9 = x_1x_2 + 9x_1x_3 + 9x_2x_3 = 0$, the points of C_9 :

{1,2,21,41,66,90,103,125,139,156,190,197,245,252,286,303,317,339,352,376}, which is a complete (20,2)-arc, since there are no points of index zero.

10. If $\alpha = 10$, then the equation of the conic $C_{10} = x_1x_2 + 10x_1x_3 + 8x_2x_3 = 0$, the points of C_{10} :

{1,2,21,41,64,82,111,126,151,163,180,226,243,255,280,295,324,342,346,366}, which is a complete (20,2)-arc, since there are no points of index zero.

11. If $\alpha = 11$, then the equation of the conic $C_{11} = x_1x_2 + 11x_1x_3 + 7x_2x_3 = 0$, the points of C_{11} :

{1,2,21,41,74,86,104,134,137,165,205,214,236,266,284,296,310,330,354,377}, which is a complete (20,2)-arc, since there are no points of index zero.

12. If $\alpha = 12$, then the equation of the conic $C_{12} = x_1x_2 + 12x_1x_3 + 6x_2x_3 = 0$, the points of C_{12} :

{1,2,21,41,69,92,105,131,152,182,203,229,242,265,274,294,309,327,349,367}, which is a complete (20,2)-arc, since there are no points of index zero.

13. If $\alpha = 13$, then the equation of the conic $C_{13} = x_1x_2 + 13x_1x_3 + 5x_2x_3 = 0$, the points of C_{13} :

{1,2,21,41,71,83,107,122,157,191,196,227,238,258,275,302,323,336,357,365}, which is a complete (20,2)-arc, since there are no points of index zero.

14. If $\alpha = 14$, then the equation of the conic $C_{14} = x_1x_2 + 14x_1x_3 + 4x_2x_3 = 0$, the points of C_{14} :

{1,2,21,41,68,84,113,149,159,175,202,222,248,253,271,304,319,333,351,375}, which is a complete (20,2)-arc, since there are no points of index zero.

15. If $\alpha = 15$, then the equation of the conic $C_{15} = x_1x_2 + 15x_1x_3 + 3x_2x_3 = 0$, the points of C_{15} :

{1,2,21,41,62,87,120,145,166,186,198,225,247,254,270,298,314,340,362,370}, which is a complete (20,2)-arc, since there are no points of index zero.

16. If $\alpha = 16$, then the equation of the conic $C_{16} = x_1x_2 + 16x_1x_3 + 2x_2x_3 = 0$, the points of C_{16} :

{1,2,21,41,63,108,130,150,160,185,208,219,232,259,273,300,313,343,347,372}, which is a complete (20,2)-arc, since there are no points of index zero.

17. If $\alpha = 17$, then the equation of the conic $C_{17} = x_1x_2 + 17x_1x_3 + x_2x_3 = 0$, the points of C_{17} :

{1,2,21,41,94,114,127,143,164,178,207,224,233,263,272,289,318,332,353,369}, which is a complete (20,2)-arc, since there are no points of index zero.

4. Existence of $[n,3,d]_{19}$ codes:

4.1 Existence of $[337,3,318]_{19}$ codes

We take one conic π , and take $\pi = PG(2,q)$ over Galois field $GF(q)$ contains 381 points and line, every line contains 20 points and every point there are 20 lines, say C_1 , let $K = \pi - C_1$

{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,

64,65,66,67,68,69,70,71,72,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,90,91,92,93,94,95,96,97,98,99,100,101,102,103,104,105,106,107,108,109,111,112,113,114,115,116,117,118,119,120,121,122,123,125,126,127,128,129,130,131,132,133,134,135,136,137,138,139,140,141,142,143,144,145,146,147,148,149,150,151,152,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,169,171,172,173,174,175,176,177,178,180,181,182,183,184,185,186,187,188,189,190,191,192,193,194,195,196,197,198,199,200,201,202,203,204,205,206,207,208,210,211,212,213,214,215,216,217,219,220,221,222,223,224,225,226,227,228,229,230,231,232,233,234,235,236,237,238,239,240,241,242,243,244,245,246,247,248,249,250,251,252,254,255,256,257,258,259,260,261,262,263,265,266,267,268,269,270,271,272,273,274,275,276,277,279,280,281,282,283,284,285,286,287,288,289,290,291,292,293,294,295,296,297,298,300,301,302,303,304,305,306,307,308,309,310,311,312,313,314,316,317,318,319,320,321,322,324,325,326,327,329,330,331,332,333,334,335,336,337,338,339,340,341,342,343,344,345,346,347,349,350,351,352,353,354,355,356,357,358,359,360,361,362,363,364,365,366,367,368,369,370,370,372,373,374,375,376,377,378,379,380,381}.

The geometrical structure method must satisfy the following :

- i. K intersects any line of π in at most 19 points .
- ii. Every point not in K is on at least one 19-secant of K .

The point :

$M = \{363, 192, 135, 287, 306, 78, 16, 173, 154, 59, 344, 249, 230, 325, 97, 116, 268, 211, 39, 317, 321, 111, 181, 66, 331, 376, 177, 221\}$ are eliminated from K to satisfy (1) . The points of index zero for 1,73,209 are added to K to satisfy (2) , then $K_{19} = K \cup \{1,73,209\} / M$

$K_{19} = \{1, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 17, 18, 19, 20, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 40, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 60, 61, 62, 63, 64, 65, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 90, 91, 92, 93, 94, 95, 96, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 112, 113, 114, 115, 117, 118, 119, 120, 121, 122, 123, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 171, 172, 174, 175, 176, 178, 180, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 212, 213, 214, 215, 216, 217, 219, 220, 222, 223, 224, 225, 226, 227, 228, 229, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 250, 251, 252, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 265, 266, 267, 269, 270, 271, 272, 273, 274, 275, 276, 277, 279, 280, 281, 282, 283, 284, 285, 286, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 300, 301, 302, 303, 304, 305, 307, 308, 309, 310, 311, 312, 313, 314, 316, 318, 319, 320, 322, 324, 326, 327, 329, 330, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 345, 346, 347, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 364, 365, 366, 367, 368, 369, 370, 370, 372, 373, 374, 375, 377, 378, 379, 380, 381\}$. Is a complete (155,13) –arc as shown in table (1) . Let $\beta_1 = \pi - k_{19}$

$= \{2, 21, 39, 41, 59, 66, 78, 89, 16, 97, 110, 111, 116, 124, 135, 153, 154, 170, 173, 177, 179, 181, 192, 211, 218, 221, 230, 249, 253, 264, 278, 287, 299, 306, 317, 321, 328, 331, 344, 348, 363, 376, 325, 315, 268\}$ is (44,1)-blocking set as shown in table (1) . β_1 is of Redei -type contains the line l_1

$= \{2, 21, 40, 59, 78, 97, 116, 135, 154, 173, 192, 211, 230, 249, 268, 287, 306, 325, 344, 363\} / \{40\}$ and one point on each line through the point 40 which are non-collinear points 42,60,79,85,112,132,107,152,126,93,145,184,164,172,198,223,233,244,257 by theorem (1) ,there exists a projective $[337,3,318]_{19}$ code which is equivalent to the complete (337,19)-arc k_{19}

Table (1)

I	$K_{19} \cap Li$	$B_1 \cap Li$
1	40	2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,287,306,325,344,363
2	1,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38	21,39
⋮	⋮	⋮
38 0	11,31,40,68,96,105,133,142,207,216,244,281,290,318,327,355,364	170,179,253
38 1	20,22,40,77,95,113,131,149,167,185,203,239,257,275,293,311,329,347,365	221

4.2 Existence of $[289,3,271]_{19}$ codes

We take two conic, say C_1, C_2 , and let $K = \pi - C_1 \cup C_2$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,67,68,69,71,72,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,90,91,92,93,94,96,97,98,100,101,102,103,104,105,106,107,108,109,111,112,113,114,115,116,117,118,119,120,121,122,123,125,126,127,128,130,131,132,133,134,135,136,137,138,139,140,141,143,144,145,146,147,148,149,150,151,152,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,171,172,173,174,175,176,177,178,180,181,182,184,185,186,187,188,189,190,191,192,193,194,195,196,197,198,199,200,201,202,203,204,205,206,207,208,211,212,213,214,215,216,217,219,220,221,222,224,225,226,227,228,229,230,231,232,233,236,237,238,239,240,241,242,243,244,245,246,247,248,249,250,251,252,253,254,255,256,258,259,260,261,262,263,265,266,267,268,269,270,271,272,273,274,275,276,277,279,280,281,283,284,285,286,287,288,289,290,291,293,294,295,296,297,298,300,301,302,303,304,305,306,307,308,309,310,311,313,314,316,317,318,319,320,321,322,323,324,325,326,327,329,330,331,332,333,335,336,337,338,339,340,341,342,343,344,345,346,347,349,350,351,352,353,354,355,356,357,358,359,360,361,362,363,364,365,366,367,368,369,370,371,372,373,374,375,376,377,378,380,381\}$. The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 18 points .
- ii. Every point not in K is on at least one 18-secant of K .

The point :

$M = \{3,9,10,11,13,15,17,363,77,112,144,192,30,177,54,184,135,300,84,47,61,100,111,199,66,86,306,225,131,78,173,161,380,154,59,322,108,333,201,18,344,52,249,350,370,230,377,325,177,97,320,311,116,268,211,40,180,106\}$ Are eliminated from K to satisfy (1)

. The points of index zero for 70,209 are added to K to satisfy (2) , then $K_{18} = K \cup$

$\{70,209\} / M$

$K_{18} = \{4,5,6,7,8,12,14,16,19,20,22,23,24,25,26,27,28,29,31,32,33,34,35,36,37,38,39,42,43,44,45,46,48,49,50,51,53,55,56,57,58,60,62,63,64,65,67,68,69,71,72,74,75,76,79,80,81,82,83,85,87,88,90,91,92,93,94,96,98,101,102,103,104,105,107,109,113,114,115,118,119,120,121,122,123,125,126,127,128,130,132,133,134,136,137,138,139,140,141,143,145,146,147,148,149,150,151,152,155,156,157,158,159,160,162,163,164,165,166,167,168,171,172,174,175,176,178,181,182,185,186,187,188,189,190,191,193,194,195,196,197,1$

98,200,202,203,204,205,206,207,208,212,213,214,215,216,217,219,220,221,222,224,226,227,228,229,231,232,233,235,236,237,238,239,240,241,242,243,244,245,246,247,248,250,251,252,254,255,256,258,259,260,261,262,263,265,266,267,269,270,271,272,273,274,275,276,277,279,280,281,283,284,285,286,287,288,289,290,291,293,294,295,296,297,298,301,302,303,304,305,307,308,309,310,313,314,316,317,318,319,321,323,324,326,327,329,330,331,332,335,336,337,338,339,340,341,342,343,345,346,347,349,351,352,353,354,355,356,357,358,359,360,361,362,364,365,366,367,368,369,371,372,373,374,375,376,378,381]. Is a complete $(289,18)$ -arc as shown in table (2). Let $\beta_2 = \pi - k_{18} = \{1,2,3,8,9,10,11,13,15,17,18,21,30,40,41,47,52,54,59,61,66,73,77,78,84,86,89,95,97,99,100,106,108,110,111,112,116,117,124,129,131,135,142,144,153,154,161,169,170,173,177,179,180,183,184,192,199,210,211,218,223,225,230,234,249,253,257,264,268,278,282,292,299,300,306,311,312,315,320,322,325,328,333,334,344,348,350,363,370,377,379,380\}$ is $(92,2)$ -blocking set as shown in table (2). by theorem (1), there exists a projective $[289,3,271]_{19}$ code which is equivalent to the complete $(289,18)$ -arc k_{18}

Table (2)

I	$K_{18} \cap Li$	$B_2 \cap Li$
1	287	2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,306,325,344,363
2	22,23,24,25,26,27,28,29,31,32,33,34,35,36,37,38,39	1,21,30
⋮	⋮	⋮
38 0	31,68,96,105,133,207,216,244,281,290,318 327,355,364	11,40,142,170,179,253
38 1	20,22,113,149,167,185,203,221,239,275,293,329,347,365	40,77,95,131,257,311

4.3 Existence of $[266,3,249]_{19}$ codes

We take 3 conic, say C_1, C_2, C_3 and let

$$K = \pi - C_1 \cup C_2 \cup C_3$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,67,68,69,71,74,75,76,77,78,79,81,82,83,84,85,86,87,88,90,91,92,93,94,96,97,98,100,101,103,104,105,106,107,108,109,111,112,113,114,115,116,117,118,119,120,121,122,123,125,126,127,130,131,132,133,134,135,136,137,138,139,140,141,143,145,146,147,148,149,150,151,152,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,171,173,174,175,176,177,178,180,181,182,184,185,186,187,189,190,191,192,193,194,196,197,198,199,200,201,202,203,204,205,206,207,208,211,212,213,214,215,216,219,220,221,222,224,225,226,227,228,229,230,231,232,233,236,237,238,239,240,241,242,243,245,246,247,248,249,250,251,252,253,254,255,258,259,260,261,262,263,265,266,267,268,269,270,271,272,273,274,275,277,279,280,281,283,284,285,286,287,288,289,290,291,293,294,295,296,298,300,301,302,303,304,305,306,307,308,309,310,311,313,314,316,317,318,319,320,321,323,324,325,326,327,329,330,331,332,333,335,336,337,338,339,340,341,342,343,344,345,346,347,349,350,351,352,353,354,356,357,358,359,360,361,362,363,364,365,366,367,368,369,370,371,372,373,374,375,376,377,378,381\}$.

The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 17 points .
- ii. Every point not in K is on at least one 17-secant of K .

The point :

M=40,22,61,10,79,363,225,100,192,320,135,350,77,177,287,30,66,306,112,54,184,131,15,84,377,199,3,333,78,130,9,13,173,161,106,154,92,180,59,8,344,11,39,111,249,370,230,20,325,171,117,50,47,97,247,373,250,113,5,186,268,181,211,222,190 Are eliminated from K to satisfy (1) . The points of index zero for 80,244 are added to K to satisfy (2) , then $K_{17} = K \cup [80,244] / M$

$K_{17} = [4,6,7,12,14,16,17,18,19,23,24,25,26,27,28,29,31,32,33,34,35,36,37,38,42,43,44,45,46,48,49,51,52,53,55,56,57,58,60,62,63,64,65,67,68,69,71,74,75,76,80,81,82,83,84,85,87,88,90,91,93,94,96,98,101,103,104,105,107,108,109,114,115,116,118,119,120,121,122,123,125,126,127,132,133,134,136,137,138,139,140,141,143,145,146,147,148,149,150,151,152,155,156,157,158,159,160,162,163,164,165,166,167,168,174,175,176,178,182,185,187,189,191,193,194,196,197,198,200,201,202,203,204,205,206,207,208,212,213,214,215,216,219,220,221,224,226,227,228,229,231,232,233,236,237,238,239,240,241,242,243,244,245,246,248,251,252,253,254,255,258,259,260,261,262,263,265,266,267,269,270,271,272,273,274,275,277,279,280,281,283,284,285,286,288,289,290,291,293,294,295,296,298,300,301,302,303,304,305,307,308,309,310,311,313,314,316,317,318,319,321,323,324,326,327,329,330,331,332,335,336,337,338,339,340,341,342,343,345,346,347,349,351,352,353,354,356,357,358,359,360,361,362,364,365,366,367,368,369,371,372,374,375,376,378,381]. Is a complete (266,17) –arc as shown in table (3) . Let $\beta_3 = \pi - k_{17}$$

$= \{1,2,3,5,8,9,10,11,13,15,20,21,22,30,39,40,41,47,50,54,59,61,66,70,72,73,77,78,79,86,89,92,95,97,99,100,102,106,110,111,112,113,117,124,128,129,130,131,135,142,144,153,154,161,169,170,171,172,173,177,179,180,181,183,184,186,188,190,192,195,199,209,210,211,217,218,222,223,225,230,234,235,247,249,250,256,257,264,268,276,278,282,287,292,297,299,306,312,315,320,322,325,328,333,334,344,348,350,355,363,370,373,377,379,380\}$ is (115,3)-blocking set as shown in table (3) .

by theorem (1) ,there exists a projective $[266,3,249]_{19}$ code which is equivalent to the complete (266,17)-arc k_{17}

Table (3)

I	$K_{17} \cap Li$	$B_3 \cap Li$
1	116	2,21,40,59,78,97,135,154,173,192,211,230,249,287,268,306,325,344,363
2	23,24,25,26,27,28,29,31,32,33,34,35,36,37,38	1,21,22,30,39
⋮	⋮	⋮
380	31,68,96,105,133,207,216,281,290,318,327,364,244,253	11,40,142,170,179,355
381	149,167,185,203,221,239,275,293,311,329,347,365	20,22,40,77,95,113,131,257

4.4 Existence of $[246,3,230]_{19}$ codes

We take 4 conic, say C_1, C_2, C_3, C_4 and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,68,69,71,74,75,76,77,78,79,81,82,83,84,85,86,87,88,90,92,93,94,96,97,98,100,101,103,104,105,106,107,108,111,112,113,114,115,116,117,118,119,120,121,122,125,126,127,130,131,132,133,134,135,136,137,139,140,141,143,145,146,147,148,149,150,151,152,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,173,174,175,176,177,178,180,181,182,184,185,186,187,190,191,192,193,196,197,198,199,200,201,202,203,204,205,206,207,208,211,212,213,214,215,216,219,221,222,224,225,226,227,228,229,230,231,232,233,236,237,238,239,241,242,243,245,246,247,248,249,250,251,252,253,254,255,258,259,260,261,262,263,265,266,268,269,270,271,272,273,274,275,277,279,280,281,284,285,286,287,288,289,290,291,294,295,296,298,300,301,302,303,304,305,306,307,308,309,310,311,313,314,316,317,318,319,320,321,323,324,325,326,327,330,331,332,333,335,336,337,338,339,340,341,342,343,344,345,346,347,349,350,351,352,353,354,356,357,359,360,361,362,363,364,365,366,367,368,369,370,371,372,373,375,376,377,378,381\}$.

The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 16 points .
- ii. Every point not in K is on at least one 16-secant of K .

The point :

$M = \{40,59,22,30,61,161,3,5,140,79,363,66,112,181,186,100,177,47,192,39,320,10,184,60,135,350,131,106,130,225,86,287,15,306,326,333,78,117,222,173,54,199,154,7,9,180,147,344,11,113,377,249,160,230,77,115,8,325,111,50,81,247,378,116,250,373,268,211,20\}$, Are eliminated from K to satisfy (1) . The points of index zero for 171,293 are added to K to satisfy (2) , then $K_{16} = K \cup [171,293] / M$

$K_{16} = \{4,6,12,13,14,16,17,18,19,23,24,25,26,27,28,29,31,32,33,34,35,36,37,38,42,43,44,45,46,48,49,51,52,53,55,56,57,58,62,63,64,65,68,69,71,74,75,76,82,83,84,85,87,88,90,92,93,94,96,97,98,101,103,104,105,107,108,114,118,119,120,121,122,125,126,127,132,133,134,136,137,139,141,143,145,146,148,149,150,151,152,155,156,157,158,159,162,163,164,165,166,167,168,171,174,175,176,178,182,185,186,187,190,191,193,196,197,198,200,201,202,203,204,205,206,207,208,212,213,214,215,216,219,221,224,226,227,228,229,231,232,233,236,237,238,239,241,242,243,245,246,248,251,252,253,254,255,258,259,260,261,262,263,265,266,269,270,271,272,273,274,275,277,279,280,281,284,285,286,288,289,290,291,293,294,295,296,298,300,301,302,303,304,305,307,308,309,310,311,313,314,316,317,318,319,321,323,324,327,330,331,332,335,336,337,338,339,340,341,342,343,345,346,347,349,351,352,353,354,356,357,359,360,361,362,364,365,366,367,368,369,370,371,372,375,376,381\}$. Is a complete $(246,16)$ –arc as shown in table (4) .

$$\text{Let } \beta_4 = \pi - k_{16}$$

$= \{1,2,3,5,7,8,9,10,11,13,15,20,21,22,30,39,40,41,47,50,54,59,60,61,66,67,70,72,73,77,78,79,80,81,86,89,91,95,99,100,102,106,109,110,111,112,113,115,116,117,123,124,128,129,130,131,135,138,140,142,144,147,153,154,160,161,169,170,172,173,177,179,180,181,183,184,186,188,189,192,194,195,199,209,210,211,217,218,220,222,223,225,230,234,235,240,244,247,249,250,256,257,264,267,268,276,278,282,283,287,292,297,299,306,312,315,320,322,325,326,328,329,333,334,344,348,350,355,358,363,373,374,377,378,379,380\}$ is $(135,4)$ -blocking set as shown in table (4) .by theorem (1) ,there exists a projective $[246,3,230]_{19}$ code which is equivalent to the complete $(246,16)$ -arc k_{16}

Table (4)

I	$K_{16} \cap Li$	$B_4 \cap Li$
1	97	2,21,40,59,78,116,135,154,173,192,211,230,249,268,287,306,325,344,363
2	23,24,25,26,27,28,29,31,32,33,34,35,36,37,38	1,22,30,39,21
⋮	⋮	⋮
380	31,68,96,105,133,207,216,281,290,318,327,364,253	11,40,142,170,179,244,355
381	149,167,185,203,293,22,239,275,311,347,365	20,22,40,77,95,113,131,257,329

4.5 Existence of $[219,3,204]_{19}$ codes

We take 5 conic, say C_1, C_2, C_3, C_4, C_5 and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,68,69,71,74,75,76,78,79,81,82,83,84,86,87,88,90,92,93,94,96,97,98,100,101,103,104,105,107,108,111,112,113,114,115,116,117,118,120,121,122,125,126,127,130,131,132,133,134,135,136,137,139,141,143,145,146,147,148,149,150,151,152,154,155,156,157,158,159,160,161,162,163,164,165,166,168,173,174,175,176,177,178,180,181,182,185,186,187,190,191,192,193,196,197,198,199,200,201,202,203,205,206,207,208,211,212,213,214,216,219,221,222,224,225,226,227,228,229,230,231,232,233,236,237,238,239,241,242,243,245,247,248,249,250,252,253,254,255,258,259,260,261,262,263,265,266,268,269,270,271,272,273,274,275,277,279,280,281,284,286,287,288,289,290,291,294,295,296,298,300,301,302,303,304,305,306,307,308,309,310,311,313,314,316,317,318,319,321,323,324,325,326,327,330,331,332,333,336,337,338,339,340,341,342,343,344,345,346,347,349,350,351,352,353,354,356,357,360,361,362,363,364,365,366,367,368,369,370,372,373,375,376,377,378,381\}$.

The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 15 points .
2. Every point not in K is on at least one 15-secant of K .

The point :

$M = \{59,78,22,30,39,61,81,161,3,5,10,197,60,79,363,20,111,112,66,181,247,57,86,131,100,186,166,177,180,47,192,347,225,377,135,130,271,115,287,54,15,190,306,199,333,222,9,173,11,381,154,7,356,101,147,121,90,344,8,249,120,230,113,174,325,69,97,18,116,370,13,250,373,321,268,211,259,155,139,378\}$

Are eliminated from K to satisfy (1) . The points of index zero for 251,359 are added to K to satisfy (2) , then $K_{15} = K \cup [251,359] / M$

$K_{15} = \{4,6,12,14,16,17,19,23,24,25,26,27,28,29,31,32,33,34,35,36,37,38,40,42,43,44,45,46,48,49,50,51,52,53,55,56,58,62,63,64,65,68,71,74,75,76,82,83,84,87,88,92,93,94,96,98,103,104,105,107,108,114,117,118,122,125,126,127,132,133,134,136,137,141,143,145,146,148,149,150,151,152,156,157,158,159,160,162,163,164,165,168,175,176,178,182,185,187,191,193,196,198,200,201,202,203,205,206,207,208,212,213,214,216,219,221,224,226,227,228,229,231,232,233,236,237,238,239,241,242,243,245,248,252,253,254,255,258,260,261,262,263,265,266,269,270,272,273,274,275,277,279,280,281,284,286,288,289,290,291,294,295,296,298,300,301,302,303,304,305,307,308,309,310,311,313,314\}$

,316,317,318,319,323,324,326,327,330,331,332,336,337,338,339,340,341,342,343,345, 346,349,350,351,352,353,354,357,360,361,362,364,365,366,367,368,369,372,375,376]. Is a complete $(219,15)$ –arc as shown in table (5) .

Let $\beta_5 = \pi - k_{15}$
 $=\{1,2,3,5,7,8,9,10,11,13,15,18,20,21,22,30,39,41,47,57,54,59,60,61,66,67,69,70,72,73, 77,78,79,80,81,85,86,89,90,91,95,97,99,100,101,102,106,109,110,111,112,113,115,116, 119,120,121,123,124,128,129,130,131,135,138,139,140,142,144,147,153,154,155,161,1 66,167,169,170,171,172,173,174,177,179,180,181,183,184,186,188,189,190,192,194,19 5,197,199,204,209,210,211,215,217,218,220,222,223,225,230,234,235,240,244,246,247 ,249,250,256,257,259,264,267,268,271,276,278,282,283,285,287,292,293,297,299,306, 312,315,320,322,321,325,328,329,333,334,335,344,347,348,355,356,358,363,370,371,3 73,374,377,378,379,380,381\}$ is $(162,15)$ -blocking set as shown in table (5) .

by theorem (1) ,there exists a projective $[219,3,204]_{19}$ code which is equivalent to the complete $(219,15)$ -arc k_{15}

Table (5)

I	$K_{15} \cap Li$	$B_5 \cap Li$
1	40	2,21,59,78,97,116,135,154,173,192,211,230,249,268,2 87,306,325,344,363
2	23,24,25,26,27,28,29,3 1,32,33,34,35,36,37,38	1,21,22,30,39
⋮	⋮	⋮
38 0	31,68,96,105,133,207, 216,281,290,318,327,3 64,253	11,40,142,170,179,244,355
38 1	149,185,203,221,239,2 75,311,365	20,22,40,77,95,113,131,167,257,293,347,329

4.6 Existence of $[206,3,192]_{19}$ codes

We take 6 conic, say $C_1, C_2, C_3, C_4, C_5, C_6$ and let

$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34 ,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63, 64,65,66,68,69,71,74,76,78,79,81,82,83,84,86,87,88,90,92,94,96,97,98,100,101,103,104 ,105,107,108,111,112,113,114,116,117,118,120,121,122,125,126,127,130,131,132,134, 135,136,137,139,141,143,145,146,147,149,150,151,152,154,155,156,157,158,159,160,1 61,162,163,164,165,166,173,174,175,176,178,180,181,182,185,186,187,190,191,192,19 3,196,197,198,199,201,202,203,205,206,207,208,211,212,214,216,219,221,222,224,225 ,226,227,228,229,230,231,232,233,236,237,238,241,242,243,245,247,248,249,250,252, 253,254,255,258,259,261,262,263,265,266,268,269,270,271,272,273,274,275,277,279,2 80,281,284,286,287,288,289,291,294,295,296,298,300,301,302,303,304,305,306,307,30 8,309,310,313,314,316,317,318,319,321,323,324,325,326,327,330,331,332,333,336,338 ,339,340,341,342,343,344,345,346,347,349,351,352,353,354,356,357,360,361,362,363, 364,365,366,367,368,369,370,372,375,376,377,378,381\}$.

The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 14 points .
2. Every point not in K is on at least one 14-secant of K .

The point :

$M=40,59,78,97,22,25,30,39,3,61,81,101,5,8,9,197,60,79,117,363,11,90,112,181,225,86,191,131,100,186,155,13,180,47,192,347,139,15,10,159,135,247,287,300,161,190,377,87,29,306,54,199,178,333,66,174,147,173,222,113,154,69,255,344,31,249,120,230,325,141,50,116,321,250,268,52,378$ Are eliminated from K to satisfy (1) . The points of index zero for 188,373 are added to K to satisfy (2) , then

$$K_{14} = K \cup [188,373] / M$$

$K_{14}=[4,6,7,12,14,16,17,18,19,20,23,24,26,27,28,32,33,34,35,36,37,38,42,43,44,45,46,48,49,51,53,55,56,57,58,62,63,64,65,68,71,74,76,82,83,84,88,92,94,96,98,103,104,105,107,108,111,114,118,121,122,125,126,127,130,132,134,136,137,143,145,146,149,150,151,152,156,157,158,160,162,163,164,165,166,175,176,182,185,187,188,193,196,198,201,202,203,205,206,207,208,211,212,214,216,219,221,224,226,227,228,229,231,232,233,236,237,238,241,242,243,245,248,252,253,254,258,259,261,262,263,265,266,269,270,271,272,273,274,275,277,279,280,281,284,286,288,289,291,294,295,296,298,301,302,303,304,305,307,308,309,310,313,314,316,317,318,319,323,324,326,327,330,331,332,336,338,339,340,341,342,343,345,346,349,351,352,353,354,356,357,360,361,362,364,365,366,367,368,369,370,372,373,375,376,381]$. Is a complete (206,14) –arc as shown in

table (6) .Let $\beta_6 = \pi - k_{14}$

$=\{1,2,3,5,8,9,10,11,13,15,21,22,25,29,30,31,39,40,41,47,50,52,54,59,60,61,66,67,69,70,72,73,75,77,78,79,80,81,85,86,87,89,90,91,93,95,97,99,100,101,102,106,109,110,112,113,115,116,117,119,120,123,124,128,129,131,133,135,138,139,140,141,142,144,147,148,153,154,155,159,161,167,168,169,170,171,172,173,174,177,178,179,180,181,183,184,186,189,190,191,192,194,195,197,199,200,204,209,210,213,215,217,218,220,222,223,225,230,234,235,239,240,244,246,247,249,250,251,255,256,257,260,264,267,268,276,278,282,283,285,287,290,292,293,297,299,300,306,311,312,315,320,321,322,325,328,329,333,334,335,337,344,347,348,350,355,358,359,363,371,374,377,378,379,380\}$ is (175,14)-blocking set as shown in table (5) .by theorem (1) ,there exists a projective $[206,3,192]_{19}$ code which is equivalent to the complete (204,14)-arc k_{14}

Table (6)

I	$K_{14} \cap Li$	$B_6 \cap Li$
1	211	2,21,40,59,78,97,116,135,173,192,230,249,268,287,306,154,325,344,363
2	23,24,26,27,28,32,33,34,35,36,37,38	1,22,25,29,30,21,31,39
⋮	⋮	⋮
380	68,96,105,207,216,281,318,327,364,253	11,31,40,133,142,170,179,244,290,355
381	20,95,149,185,203,221,275,365	40,22,77,113,131,167,239,257,293,311,329,347

4.7 Existence of $[181,3,168]_{19}$ codes

We take 7 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7$ and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,66,68,69,71,74,76,78,79,81,82,83,84,86,87,90,92,94,96,97,98,100,101,103,104,105,107,108,111,113,114,116,117,118,120,121,122,125,126,127,130,131,134,135,136,137,13$

9,141,143,145,147,149,150,151,152,154,155,156,157,159,160,161,162,163,164,165,166,173,174,175,178,180,181,182,185,186,187,190,191,192,193,196,197,198,199,201,202,203,205,207,208,211,212,214,216,219,221,222,224,225,226,227,229,230,231,232,233,236,238,241,242,243,245,247,248,249,250,252,253,254,255,258,259,261,262,263,265,266,268,269,270,271,272,273,274,275,279,280,281,284,286,287,288,289,291,294,295,296,298,300,301,302,303,304,306,307,309,310,313,314,316,317,318,319,321,323,324,325,326,327,330,331,332,333,336,339,340,341,342,343,344,345,346,347,349,351,352,353,354,357,360,361,362,363,364,365,366,367,369,370,372,375,376,377,378,381}.

The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 13 points .
2. Every point not in K is on at least one 13-secant of K .

The point :

$M = \{40,59,78,97,116,22,79,90,103,25,30,31,39,31,6,81,161,181,5,7,9,10,197,60,250,174,363,333,247,86,131,100,186,166,13,192,347,180,225,139,135,130,287,69,47,377,15,190,242,306,199,178,111,66,117,54,121,173,222,259,154,378,52,101,20,191,381,11,150,187,159,74,8,249,120,352,147,230,325,137,141,370,268,211,50,87\}$ are eliminated from K to satisfy (1) . The points of index zero for 209,210 are added to K to satisfy (2) , then $K_{13} = K \cup [209,210] / M$

$K_{13} = \{4,6,12,14,16,17,18,19,23,24,26,27,28,29,32,33,34,35,36,37,38,42,43,44,45,46,48,49,51,53,55,56,57,58,62,63,64,68,71,76,82,83,84,92,94,96,98,104,105,107,108,113,114,118,122,125,126,127,134,136,143,145,149,151,152,155,156,157,160,162,163,164,165,175,182,185,193,196,198,201,202,203,205,207,208,209,210,212,214,216,219,221,224,226,227,229,231,232,233,236,238,241,243,245,248,252,253,254,255,258,261,262,263,265,266,269,270,271,272,273,274,275,279,280,281,284,286,288,289,291,294,295,296,298,300,301,302,303,304,307,309,310,313,314,316,317,318,319,321,323,324,326,327,330,331,332,336,339,340,341,342,343,344,345,346,349,351,353,354,357,360,361,362,364,365,366,367,369,372,375,376\}$.

Is a complete $(181,13)$ -arc as shown in table (7) .Let $\beta_7 = \pi - k_{13}$
 $= \{1,2,3,5,7,8,9,10,11,13,15,20,21,22,25,30,31,39,40,41,47,50,52,54,59,60,61,65,66,67,69,70,72,73,74,75,77,78,79,80,81,85,86,87,88,89,90,91,93,95,97,99,100,101,102,103,106,109,110,111,112,115,116,117,119,120,121,123,124,128,129,130,131,132,133,135,137,138,139,140,141,142,144,146,147,148,150,153,154,158,159,161,166,167,168,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,200,204,206,211,213,215,217,218,220,222,223,225,228,230,234,235,237,239,240,242,244,246,247,249,250,251,253,256,257,259,260,264,267,268,276,277,278,282,283,285,287,290,292,293,297,299,305,306,308,311,312,315,320,322,325,328,329,333,334,335,337,338,347,348,350,352,355,356,358,359,363,368,370,371,373,374,377,378,379,380,381\}$ is $(200,13)$ -blocking set as shown in table (7) .by theorem (1) ,there exists a projective $[181,3,168]_{19}$ code which is equivalent to the complete $(181,13)$ -arc k_{13}

Table (7)

I	$K_{13} \cap Li$	$B_7 \cap Li$
1	344	2,21,40,59,78,97,116,145,173,192,211,230,249,268,287,135,306,325,363
2	23,24,26,27,28,29,32,33,34,35,36,37,38	1,21,22,25,30,31,39
⋮	⋮	⋮

380	68,96,105,207,216,281,318,327,364,253	11,31,40,133,142,170,179,244,290,355
381	113,149,185,203,221,275,365	20,22,40,77,167,95,131,293,239,257,311,329,347

4.8 Existence of $[157,3,145]_{19}$ codes

We take 8 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8$ and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,66,68,69,71,74,78,79,81,82,83,84,86,87,90,92,94,97,98,101,103,104,105,107,108,111,113,114,116,117,120,121,122,125,126,127,130,131,134,135,136,137,139,141,143,145,149,150,151,152,154,155,156,157,159,160,161,163,164,165,166,173,174,175,178,180,181,182,185,186,190,191,192,193,196,197,198,201,202,203,205,207,208,211,212,214,219,221,222,224,225,226,227,229,230,231,232,233,236,238,241,242,243,245,247,248,249,250,252,253,254,255,258,259,261,263,265,266,268,269,270,271,272,273,274,275,280,281,284,286,287,288,289,294,295,296,298,300,301,302,303,304,306,307,309,310,313,314,317,318,319,321,323,324,325,326,327,330,332,333,336,339,340,341,342,343,344,345,346,347,349,351,352,353,354,357,361,362,363,364,365,366,367,369,370,372,375,376,377,381\}$.

The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 12 points .
- ii. Every point not in K is on at least one 12-secant of K .

The point :

$M = \{40,59,78,97,116,135,22,25,30,31,29,39,16,3,5,7,9,10,61,81,101,161,181,8,6,15,178,197,60,79,117,174,250,20,363,66,130,86,186,131,13,166,192,180,191,14,300,333,225,121,54,287,69,47,19,190,87,306,377,111,18,139,381,259,173,90,11,201,222,114,154,52,247,347,370,301,344,159,303,343,249,120,339,152,230,310,311,325,107,50,141,271,125,56,231\}$ Are eliminated from K to satisfy (1) . The points of index zero for 311,312 are added to K to satisfy (2) , then $K_{12} = K \cup [311,312] / M$

$K_{12} = \{4,17,23,24,26,27,28,32,33,34,35,36,37,38,42,43,44,45,46,48,49,51,53,55,57,58,62,63,64,68,71,74,82,83,84,92,94,98,103,104,105,108,113,122,125,126,127,134,136,137,143,145,149,150,151,155,156,157,160,163,164,165,175,182,185,193,196,198,202,203,205,207,208,211,212,214,219,221,224,226,227,229,232,233,236,238,241,242,243,245,248,252,253,254,255,258,261,263,265,266,268,269,270,272,273,274,275,280,281,284,286,288,289,294,295,296,298,302,304,307,309,311,312,313,314,317,318,319,321,323,324,326,327,330,332,336,340,341,342,345,346,349,351,352,353,354,357,361,362,364,365,366,367,369,372,375,376\}$. Is a complete $(157,12)$ –arc as shown in table (8) . Let $\beta_8 = \pi - k_{12}$

$= \{1,2,3,5,6,7,8,9,10,11,12,13,14,15,16,18,19,20,21,22,25,29,30,31,39,40,41,47,50,52,54,56,59,60,61,65,66,67,69,70,72,73,75,76,77,78,79,80,81,85,86,87,88,89,90,91,93,95,96,97,99,100,101,102,106,107,109,110,111,112,114,115,116,117,118,119,120,121,123,124,128,129,130,131,132,133,135,138,139,140,141,142,144,146,147,148,152,153,154,158,159,161,162,166,167,168,169,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,200,201,204,206,209,210,211,213,215,216,217,218,220,222,223,225,228,230,231,234,235,237,239,240,244,246,247,249,250,251,256,257,259,260,262,264,267,271,276,277,278,279,282,283,285,287,290,291,292,293,297,299,300,301,303,305,306,308,310,315,316,320,322,325,328,329,331,333,334,335,$

$\{337,338,339,343,344,347,348,350,355,356,358,359,360,363,368,370,371,373,374,377,378,379,380,381\}$ is $(200,12)$ -blocking set as shown in table (8) .

by theorem (1) ,there exists a projective $[157,3,145]_{19}$ code which is equivalent to the complete $(157,12)$ -arc k_{12}

Table (8)

I	$K_{12} \cap Li$	$B_8 \cap Li$
1	268	2,21,40,59,78,97,116,135,154,173,192,211,249,287,306,325,344,363,230
2	23,24,26,27,28,32,33,34,35,36,37,38	1,21,22,25,30,31,29,39
⋮	⋮	⋮
380	68,105,207,281,318,327,364,253	11,31,40,96,133,142,170,179,216,244,290,355
381	113,149,185,311,203,221,275,365	20,22,40,77,95,131,167,239,257,293,347,329

4.9 Existence of $[141,3,130]_{19}$ codes

We take 9 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9$ and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9$$

$\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,64,68,69,71,74,78,79,81,82,83,84,86,87,92,94,97,98,101,104,105,107,108,111,113,114,116,117,120,121,122,126,127,130,131,134,135,136,137,141,143,145,149,150,151,152,154,155,157,159,160,161,163,164,165,166,173,174,175,178,180,181,182,185,186,191,192,193,196,198,201,202,203,205,207,208,211,212,214,219,221,222,224,225,226,227,229,230,231,232,233,236,238,241,242,243,247,248,249,250,253,254,255,258,259,261,263,265,266,268,269,270,271,272,273,274,275,280,281,284,287,288,289,294,295,296,298,300,301,302,304,306,307,309,310,313,314,318,319,321,323,324,325,326,327,330,332,333,336,340,341,342,343,344,345,346,347,349,351,353,354,357,361,362,363,364,365,366,367,369,370,372,375,377,381\}$.

The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 11 points .
- ii. Every point not in K is on at least one 11-secant of K .

The point :

$M = \{40,59,78,97,116,135,20,154,22,25,30,31,39,35,3,61,81,101,141,161,181,5,7,9,10,12,14,159,178,121,60,79,117,174,250,155,363,333,160,225,191,86,107,186,166,300,192,180,130,52,15,16,54,13,38,287,69,47,19,151,87,306,377,347,50,111,18,222,255,104,173,247,131,259,11,4,344,150,159,344,343,8,120,152,370,230,301,114,325,17,207,268,211\}$ Are eliminated from K to satisfy (1) . The points of index zero for 251,252 are added to

K to satisfy (2) , then $K_{11} = K \cup [251,252] / M$

$K_{11} = \{6,23,24,26,27,28,32,33,34,36,37,38,42,43,44,45,46,48,49,51,53,55,57,62,63,64,68,71,74,82,83,84,92,94,98,105,108,113,122,126,127,134,136,137,143,145,149,157,163,164,165,175,182,185,193,196,198,201,202,203,205,208,212,214,219,221,224,226,227,229,231,232,233,236,238,241,242,243,248,249,251,252,253,254,258,261,263,265,266,269,270,271,272,273,274,275,280,281,284,288,289,294,295,296,298,302,304,307,309,310,313,314,318,319,321,323,324,326,327,330,332,336,340,341,342,345,346,349,351,353,354,357,361,362,364,365,366,367,369,372,375\}$. Is a complete $(141,11)$ –arc as shown in table (9) . Let $\beta_9 = \pi - k_{11}$

={1,2,3,4,5,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,25,29,30,31,35,39,40,41,47,50,52,54,56,58,59,60,61,65,66,67,69,70,72,73,75,76,77,78,79,80,81,85,86,87,88,89,90,91,93,95,96,97,99,100,101,102,103,104,106,107,109,110,111,112,114,115,116,117,118,119,120,121,123,124,125,128,129,130,130,132,133,135,138,139,140,141,142,144,146,147,148,150,151,152,153,154,155,156,158,159,160,161,162,166,167,168,169,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,200,204,206,207,209,210,211,213,215,216,217,218,220,222,223,225,228,230,234,235,237,239,240,244,245,246,247,250,255,256,257,259,260,262,264,267,268,276,277,278,279,282,283,285,286,287,290,291,292,293,297,299,300,301,303,305,306,308,311,312,315,316,317,320,322,325,328,329,331,333,334,335,337,338,339,343,344,347,348,350,352,355,356,358,359,360,363,368,370,371,373,374,376,377,378,379,380,381} is (240,11)-blocking set as shown in table (9) .

by theorem (1) ,there exists a projective $[141,3,130]_{19}$ code which is equivalent to the complete $(141,11)$ -arc k_{11}

Table (9)

I	$K_{11} \cap Li$	$B_9 \cap Li$
1	249	2,21,40,59,78,97,116,135,154,173,192,211,230,268,287,306,344,325,363
2	23,24,26,27,28,32,33,34,36,37,38	1,21,25,29,30,31,35,39,22
⋮	⋮	⋮
380	68,105,281,318,327,364,253	11,31,40,96,133,142,170,179,207,216,244,290,355
381	113,149,185,203,221,275,365	20,22,40,77,131,167,239,257,95,239,311,329,347

4.10 Existence of $[120,3,110]_{19}$ codes

We take 10 conic , say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}$ and let $K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10}$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,68,69,71,74,78,79,81,83,84,86,87,92,94,97,98,101,104,105,107,108,113,114,116,117,120,121,122,127,130,131,134,135,136,137,141,143,145,149,150,152,154,155,157,159,160,161,164,165,166,173,174,175,178,181,182,185,186,191,192,193,196,198,201,202,203,205,207,208,211,212,214,219,221,222,224,225,227,229,230,231,232,233,236,238,241,242,247,248,249,250,253,254,258,259,261,263,265,266,268,269,270,271,272,273,274,275,281,284,287,288,289,294,296,298,300,301,302,304,306,307,309,310,313,314,318,319,321,323,325,326,327,330,332,333,336,340,341,343,344,345,347,349,351,353,354,357,361,362,363,364,365,367,369,370,372,375,377,381\}$. The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 10 points .
- ii. Every point not in K is on at least one 10-secant of K .

The point :

$M = \{40,59,78,97,116,135,154,173,22,25,29,30,31,33,35,39,3,61,81,101,121,141,161,181,5,9,10,12,14,16,20,60,79,117,155,174,250,231,363,160,130,247,225,87,191,86,107,4,186,300,259,166,13,192,69,15,54,178,47,19,134,104,58,375,330,232,377,74,306,50,222,347,150,11,136,201,52,301,381,344,159,307,249,120,152,108,370,230,18,114,340,325,2$

07,17,270,268,211,40,310 Are eliminated from K to satisfy (1) . The points of index zero for 65,66 are added to K to satisfy (2) , then $K_{10} = K \cup [65,66] / M$
 $K_{10} = [6,7,8,23,24,26,27,28,32,34,36,37,38,42,43,45,46,48,49,51,53,55,56,57,62,63,65,66,68,71,83,84,92,94,98,105,113,122,127,131,137,143,145,149,157,164,165,175,182,185,193,196,198,202,203,205,208,212,214,219,221,224,227,229,233,236,238,241,242,248,253,254,258,261,263,265,266,269,271,272,273,274,275,281,284,287,288,289,294,296,298,302,304,309,313,314,318,319,321,323,326,327,332,333,336,341,343,345,349,351,353,354,357,361,362,364,365,367,369,372]$. Is a complete $(120,10)$ -arc as shown in table (10) .Let $\beta_{10} = \pi - k_{10}$
 $= \{1,2,3,4,5,9,10,11,12,13,14,15,16,17,18,19,20,21,22,25,29,30,31,33,35,39,40,41,44,47,50,52,54,58,59,60,61,64,67,69,70,72,73,74,75,76,77,78,79,80,81,82,85,86,87,88,89,90,91,93,95,96,97,99,100,101,102,103,104,106,107,108,109,110,111,112,114,115,116,117,118,119,120,121,123,124,125,126,128,129,130,132,133,134,135,136,138,139,140,141,142,144,146,147,148,150,151,152,153,154,155,156,158,159,160,161,162,163,166,167,168,169,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,200,201,204,206,207,209,210,211,213,215,216,217,218,220,222,223,225,226,228,230,231,232,234,235,237,239,240,243,244,245,246,247,249,250,251,252,255,256,257,259,260,262,264,267,268,270,276,277,278,279,280,282,283,285,286,290,291,292,293,295,297,299,300,301,303,305,306,307,308,310,311,312,315,316,317,320,322,324,325,328,329,330,331,334,335,337,338,339,340,342,344,346,347,348,350,352,355,356,358,359,360,363,366,368,370,371,373,374,375,376,377,378,379,380,381\}$ is $(261,11)$ -blocking set as shown in table (10) .by theorem (1) ,there exists a projective $[120,3,110]_{19}$ code which is equivalent to the complete $(120,10)$ -arc k_{10}

Table (10)

I	$K_{10} \cap Li$	$B_{10} \cap Li$
1	287	2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,306,325,344,363
2	23,24,26,27,28,32,34,36,37,38	1,21,22,25,29,30,31,33,35,39
⋮	⋮	⋮
380	68,105,281,318,327,364,253	11,31,40,96,133,142,170,179,207,216,244,290,355
381	113,149,185,203,221,275,365	20,22,40,77,95,131,167,239,257,293,311,329,347

4.11 Existence of $[112,3,103]_{19}$ codes

We take 11 conic , say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}$ and let $K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11}$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,68,69,71,78,79,81,83,84,87,92,94,97,98,101,105,107,108,113,114,116,117,120,121,122,127,130,131,135,136,141,143,145,149,150,152,154,155,157,159,160,161,164,166,173,174,175,178,181,182,185,186,191,192,193,196,198,201,202,203,207,208,211,212,219,221,222,224,225,227,229,230,231,232,233,238,241,242,247,248,249,250,253,254,258,259,261,263,265,268,269,270,271,272,273,274,275,281,287,288,289,294,298,300,301,302,304,306,307,309,313,314,318,319,321,323,325,326,327,332,333,336,340,341,343,344,3$

45,347,349,351,353,357,361,362,363,364,365,367,369,370,372,375,381 }.

The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 9 points .
2. Every point not in K is on at least one 9-secant of K .

The point :

$M=40,59,78,97,116,135,154,173,192,22,25,29,30,31,33,35,39,36,3,61,81,101,121,5,6,7,10,9,12,14,16,41,161,181,381,60,79,117,155,174,250,307,363,333,160,130,20,191,107,44,4,300,207,166,136,47,186,178,52,114,341,87,6,15,247,113,287,69,54,58,306,18,159,347,222,150,259,271,50,11,201,225,344,343,249,289,108,19,370,230,268,211$ Are

eliminated from K to satisfy (1) . The points of index zero for 216,217 are added to K to satisfy (2) , then $K_9 = K \cup \{216,217\} / M$

$K_9 = \{8,13,17,23,24,26,27,28,32,34,37,38,42,43,45,46,48,49,51,53,55,56,57,62,63,68,71,83,84,92,94,98,105,120,122,127,131,143,145,149,152,157,164,175,182,185,193,196,198,202,203,208,212,216,217,219,221,224,227,229,231,232,233,238,241,242,248,253,254,258,261,263,265,269,270,272,273,274,275,281,288,294,298,301,302,304,309,313,314,318,319,321,323,325,326,327,332,336,340,345,349,351,353,357,361,362,364,365,367,369,372,375\}$. Is a complete (112,9) –arc as shown in table (11) . Let $\beta_{11} = \pi - k_9$

$= \{1,2,3,4,5,6,7,9,10,11,12,14,15,16,18,19,20,21,22,25,29,30,31,33,35,36,39,40,41,44,47,49,50,52,54,56,58,59,60,61,64,65,66,67,69,70,72,73,74,75,76,77,78,79,80,81,82,85,86,87,88,89,90,91,93,95,96,97,99,100,101,102,103,104,106,107,108,109,110,111,112,113,114,115,116,117,118,119,121,123,124,125,126,128,129,130,132,133,134,135,136,137,138,139,140,141,142,144,146,147,148,150,151,153,154,155,156,158,159,160,161,162,163,165,166,167,168,169,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,200,201,204,205,206,207,209,210,211,213,214,215,,218,220,222,223,225,226,228,230,234,235,236,237,239,240,243,244,245,246,247,249,250,251,252,254,255,256,257,259,260,262,264,266,267,268,271,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,295,296,297,299,300,303,305,306,307,308,310,311,312,315,316,317,320,322,324,328,329,330,331,333,334,335,337,338,339,341,342,343,344,346,347,348,350,352,354,355,356,358,359,360,363,366,368,370,371,373,374,376,377,378,379,380,381\}$ is (269,9)-blocking set as shown in table (11) . by theorem (1) ,there exists a projective $[112,3,103]_{19}$ code which is equivalent to the complete (112,9)-arc k_9

Table (11)

I	$K_9 \cap Li$	$B_{11} \cap Li$
1	325	2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,287,306,344,363
2	23,24,26,27,28,32,34,37,38	1,21,22,25,29,30,31,33,35,36,39
⋮	⋮	⋮
380	68,105,281,318,327,364,216,253	11,31,40,96,133,142,170,179,207,244,290,355
381	149,185,131,203,221,275	20,22,40,77,95,113,167,239,257,293,311,329,347,365

4.12 Existence of $[82,3,74]_{19}$ codes

We take 12 conic , say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}$ and let $K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12}$

{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,68,71,78,79,81,83,84,87,94,97,98,101,107,108,113,114,116,117,120,121,122,127,130,135,136,141,143,145,149,150,154,155,157,159,160,161,164,166,173,174,175,178,181,185,186,191,192,193,196,198,201,202,207,208,211,212,219,221,222,224,225,227,230,231,232,233,238,241,247,248,249,250,253,254,258,259,261,263,268,269,270,271,272,273,275,281,287,288,289,298,300,301,302,304,306,307,313,314,318,319,321,323,325,326,332,333,336,340,341,343,344,345,347,351,353,357,361,362,363,364,365,369,370,372,375,381}.

The geometrical Structure method must satisfy the following :

- K intersects any line of π in at most 8 points .
- Every point not in K is on at least one 8-secant of K .

The point : $M=40,59,78,97,116,135,154,173,192,211,22,24,25,29,30,31,33,35,36,39,3,61,81,101,121,161,181,201,301,381,4,5,6,7,8,10,12,14,20,60,79,117,136,155,174,250,307,269,363,17,130,160,9,54,44,107,191,300,259,207,166,178,225,16,15,50,108,87,52,114,289,186,58,56,287,19,47,340,122,150,347,120,222,113,159,18,247,333,271,302,344,343,249,141,370,26,49,230,325,34,270,268,336,45,37$. Are eliminated from K to satisfy (1) . The points of index zero for 200,300 are added to K to satisfy (2), then $K_8 = K \cup [200,300] / M$

$K_8=[11,13,23,27,28,32,38,42,43,46,48,51,53,55,57,62,63,68,71,83,84,94,98,127,143,145,149,157,164,175,185,193,196,198,200,202,208,212,219,221,224,227,231,232,233,238,241,248,253,254,258,261,263,272,273,275,281,288,298,300,304,306,313,314,318,319,321,323,326,332,341,345,351,353,357,361,362,364,365,369,372,375]$. Is a complete

$(82,8)$ -arc as shown in table (12) .Let $\beta_{12} = \pi - k_8$
 $=\{1,2,3,4,5,6,7,8,9,10,12,14,15,16,17,18,19,20,21,22,24,25,26,29,30,31,33,34,35,36,37,39,40,41,44,45,47,49,50,52,54,56,58,59,60,61,64,65,66,67,69,70,72,73,74,75,76,77,78,79,80,81,82,85,86,87,88,89,90,91,92,93,95,96,97,99,100,101,102,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,118,119,121,122,123,124,125,126,128,129,130,131,132,133,134,135,136,137,138,139,140,141,142,144,146,147,148,150,151,152,153,154,155,156,158,159,160,161,162,163,165,166,167,168,169,170,171,172,173,174,176,177,178,179,180,181,183,184,186,187,188,189,190,191,192,194,195,197,199,201,203,204,205,206,207,209,210,211,213,214,215,216,217,218,220,222,223,225,226,228,229,230,234,235,236,237,239,240,242,243,244,245,246,247,249,250,251,252,255,256,257,259,260,262,264,265,266,267,268,269,270,271,274,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,294,295,296,297,299,301,302,303,305,306,307,308,309,310,311,312,315,316,317,320,322,324,325,327,328,329,330,331,333,334,335,336,337,338,339,340,342,343,344,346,347,348,349,350,352,354,355,356,358,359,360,363,366,367,368,370,371,373,374,376,377,378,379,380,381}$ is $(299,8)$ -blocking set as shown in table (12) .by theorem (1) ,there exists a projective $[82,3,74]_{19}$ code which is equivalent to the complete $(82,8)$ -arc k_8

Table (12)

I	$K_8 \cap Li$	$B_{12} \cap Li$
1	306	2,21,40,59,78,97,116,135,154,173,192,211,230,249,268,287,325,344,363
2	23,27,28,32,38	1,21,22,24,25,26,29,30,31,33,34,35,36,37,39
⋮	⋮	⋮
38	11,68,281,318,364,	31,40,96,105,133,142,170,179,207,216,244,290,327,355

0	253	
38	149,185,221,275,36	20,22,40,77,95,113,131,347,329,167,203,239,257,293,311
1	5	

4.13 Existence of [72,3,65]₁₉ codes

We take 13 conic , say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}, C_{13}$ and let $K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12} \cup C_{13}$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,68,78,79,81,84,87,94,97,98,101,108,113,114,116,117,120,121,127,130,135,136,141,143,145,149,150,154,155,159,160,161,164,166,173,174,175,178,181,185,186,192,193,198,201,202,207,208,211,212,219,221,222,224,225,230,231,232,233,241,247,248,249,250,253,254,259,261,263,268,269,270,271,272,273,281,287,288,289,298,300,301,304,306,307,313,314,318,319,321,325,326,332,333,340,341,343,344,345,347,351,353,361,362,363,364,369,370,372,375,381\}$. The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 7 points .
2. Every point not in K is on at least one 7-secant of K .

The point :

$M = \{40,59,78,97,116,135,154,173,211,230,22,24,25,26,27,29,30,31,33,35,39,249,61,3,81,101,121,141,161,181,201,301,381,4,5,6,7,8,10,12,60,79,117,136,155,174,14,16,20,250,269,307,345,363,178,17,36,130,136,333,247,225,9,54,44,340,186,13,166,207,259,300,347,222,150,164,15,50,108,52,87,114,289,287,306,120,18,58,271,11,344,325,343,268,45,47,49,175,46\}$. Are eliminated from K to satisfy (1) . The points of index zero for $112,312$ are added to K to satisfy (2) , then $K_7 = K \cup [112,312] / M$
 $K_7 = \{19,23,28,32,34,37,38,42,43,48,51,53,55,56,57,62,63,68,84,94,98,112,113,127,143,145,149,159,185,192,193,198,202,208,212,219,221,224,231,232,233,241,248,253,254,261,263,270,272,273,281,288,298,304,312,313,314,318,319,321,326,332,341,351,353,361,362,364,369,370,372,375\}$. Is a complete $(72,7)$ –arc as shown in table (13) .Let

$\beta_{13} = \pi - k_7$
 $= \{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,20,21,22,24,25,26,27,29,30,31,33,35,36,39,40,41,44,45,46,47,49,50,52,54,58,59,60,61,64,65,66,67,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,85,86,87,88,89,90,91,92,93,95,96,97,99,100,101,102,103,104,105,106,107,108,109,110,111,114,115,116,117,118,119,121,122,123,124,125,126,128,129,130,131,132,133,134,135,136,137,138,139,140,141,142,144,146,147,148,150,151,152,153,154,155,156,157,158,160,161,162,163,164,165,166,167,168,169,170,171,172,173,174,175,176,177,178,179,180,181,182,183,184,186,187,188,189,190,191,192,194,195,196,197,199,200,201,203,204,205,206,207,209,210,211,213,214,215,216,217,218,220,222,223,225,226,227,228,229,230,234,235,236,237,238,239,240,242,243,244,245,246,247,249,250,251,252,255,256,257,258,259,260,262,264,265,266,267,268,269,271,274,275,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,294,295,296,297,299,301,302,303,305,306,307,308,309,310,311,315,316,317,320,322,323,324,325,327,328,329,330,331,333,334,335,336,337,338,339,340,342,343,344,345,346,347,348,349,350,352,354,355,356,357,358,359,360,363,365,366,367,368,371,373,374,376,377,378,379,380,381\}$ is $(309,7)$ -blocking set as shown in table (13).by theorem (1) ,there exists a projective $[72,3,65]_{19}$ code which is equivalent to the complete $(72,7)$ -arc k_7

Table (13)

I	$K_7 \cap Li$	$B_{13} \cap Li$
1	192	2,21,40,59,78,97,116,135,154,173,211,230,249,268,287,306,325,344,363
2	23,28,32,34,37	1,21,22,24,25,26,27,29,30,31,33,35,36,38,39
⋮	⋮	⋮
38 0	68,281,318,364,253	11,31,40,96,105,133,142,170,179,207,216,244,290,327,355
38 1	113,149,185,221	20,22,40,77,95,131,167,203,239,347,365,257,275,293,311,329

4.14 Existence of $[54,3,48]_{19}$ codes

We take 14 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}, C_{13}, C_{14}$ and let $K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12} \cup C_{13} \cup C_{14} \{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,78,79,81,87,94,97,98,101,108,114,116,117,120,121,127,130,135,136,141,143,145,150,154,155,160,161,164,166,173,174,178,181,185,186,192,193,198,201,207,208,211,212,219,221,224,225,230,231,232,233,241,247,249,250,254,259,261,263,268,269,270,272,273,281,287,288,289,298,300,301,306,307,313,314,318,321,325,326,332,340,341,343,344,345,347,353,361,362,363,364,369,370,372,381\}$. The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 6 points .
- ii. Every point not in K is on at least one 6-secant of K .

The point :

$M = \{40,59,78,97,116,154,173,192,211,230,249,268,22,24,25,26,27,28,29,30,31,33,35,39,3,61,81,101,121,141,161,181,201,301,381,341,4,5,6,7,8,9,10,12,14,16,20,60,79,117,136,155,174,250,269,307,345,231,363,160,130,36,247,186,340,300,259,207,166,47,225,178,164,150,108,343,289,114,87,127,370,58,49,56,287,306,19,344,120,13,11,325,270,48,44,45,45,50,52,54,37\}$ Are eliminated from K to satisfy (1) . The points of index zero for 171,271 are added to K to satisfy (2) , then $K_6 = K \cup \{171,271\} / M$

$K_6 = \{15,17,18,23,32,34,38,42,43,51,53,55,57,62,63,94,98,135,143,145,171,185,193,198,208,212,219,221,224,232,233,241,254,261,263,271,272,273,281,288,298,313,314,318,321,326,332,347,353,361,362,364,369,372\}$. Is a complete (54,6) –arc as shown in table

(14) . Let $\beta_{14} = \pi - k_6$

$= \{1,2,3,4,5,6,7,8,9,10,11,12,13,14,16,19,20,21,22,24,25,26,27,28,29,30,31,33,35,36,37,39,40,41,44,45,46,47,48,49,50,52,54,56,58,59,60,61,64,65,66,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,89,90,91,92,93,95,96,97,99,100,101,102,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,118,119,120,121,122,123,124,125,126,127,128,129,130,131,132,133,134,136,137,138,139,140,141,142,144,146,147,148,149,150,151,152,153,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,169,170,172,173,174,175,176,177,178,179,180,181,182,183,184,186,187,188,189,190,191,192,194,195,196,197,199,200,201,202,203,204,205,206,207,209,210,211,213,214,215,216,217,218,220,222,223,225,226,227,228,229,230,231,234,235,236,237,238,239,240,242,243,244,245,246,247,248,249,250,251,252,253,255,256,257,258,259,260,262,264,265,266,267,268,269,270,274,275,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,294,295,296,297,299,301,302,303,304,305,306,307,308,309,310,311,312,315,316,317,319,320,322,323,324,325,327,328,329,330,331,333,334,335,336,33$

7,338,339,340,341,342,343,344,345,346,348,349,350,351,352,354,355,356,357,358,359,360,363,365,366,367,368,370,371,373,374,376,377,378,379,380,381} is (327,6)-blocking set as shown in table (14) .

by theorem (1) ,there exists a projective $[54,3,48]_{19}$ code which is equivalent to the complete (54,6)-arc k_6

Table (14)

I	$K_6 \cap Li$	$B_{14} \cap Li$
1	135	2,21,40,59,78,97,116,154,173,192,211,230,249,268,287,306,325,344,363
2	23,34,38	1,21,22,24,25,26,27,28,29,30,31,32,33,35,36,37,39
⋮	⋮	⋮
38 0	281,318,364	11,31,40,68,96,105,133,142,170,179,207,216,244,253,290,327,355
38 1	185,221	20,22,40,77,95,113,131,149,167,95,347,329,203,239,257,275,293,311

4.15 Existence of $[37,3,32]_{19}$ codes

We take 15 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}, C_{13}, C_{14}, C_{15}$ and let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12} \cup C_{13} \cup C_{14} \cup C_{15}$$

{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,63,78,79,81,94,97,98,101,108,114,116,117,121,127,130,135,136,141,143,150,154,155,160,161,164,173,174,178,181,185,192,193,201,207,208,211,212,219,221,224,230,231,232,233,241,249,250,259,261,263,268,269,272,273,281,287,288,289,300,301,306,307,313,318,321,325,326,332,341,343,344,345,347,353,361,363,364,369,372,381}.

The geometrical Structure method must satisfy the following :

1. K intersects any line of π in at most 5 points .
2. Every point not in K is on at least one 5-secant of K .

The point :

$M = \{40,59,78,97,116,135,154,192,211,230,249,268,306,22,24,25,27,28,29,30,31,33,35,36,38,39,18,3,61,81,101,121,141,161,181,201,301,341,361,381,4,5,6,7,8,10,12,14,16,20,9,11,60,79,117,136,155,174,250,269,307,345,231,193,363,130,300,259,207,347,50,150,164,108,114,26,212,48,160,343,47,54,17,127,232,49,37,58,45,173,289,32,344,43,325,15,34,42,46,52,56,241\}$ Are eliminated from K to satisfy (1) . The points of index zero for 102,240 are added to K to satisfy (2) , then $K_5 = K \cup [102,240] / M$

$K_5 = \{13,19,23,44,51,53,55,57,63,94,98,102,143,178,185,208,219,221,224,233,240,261,263,272,273,281,287,288,313,318,321,326,332,353,364,369,372\}$ Is a complete (37,5) – arc as shown in table (15) .Let $\beta_{15} = \pi - k_5$

$= \{1,2,3,4,5,6,7,8,9,10,11,12,14,16,20,21,22,24,25,26,27,28,29,30,31,32,33,34,35,36,37,39,40,41,42,43,45,46,47,48,49,50,52,54,56,58,59,60,61,62,64,65,66,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,89,90,91,92,93,95,96,97,99,100,101,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,118,119,120,121,122,123,124,125,126,127,128,129,130,131,132,133,134,135,136,137,138,139,140,141,142,144,145,146,147,148,149,150,151,152,153,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,169,170,171,172,173,174,175,176,177,179,180,181,182,183,184,186,187,188,189,190,191,192,193,194,195,196,197,198,199,200,201,202,203,204,205,206,207$

,209,210,211,212,213,214,215,216,217,218,220,222,223,225,226,227,228,229,230,231, 232,234,235,236,237,238,239,241,242,243,244,245,246,247,248,249,250,251,252,253,2 54,255,256,257,258,259,260,262,264,265,266,267,268,269,270,271,274,275,276,277,27 8,279,280,282,283,284,285,286,289,290,291,292,293,294,295,296,297,298,299,300,301 ,302,303,304,305,306,307,308,309,310,311,312,314,315,316,317,319,320,322,323,324, 325,327,328,329,330,331,333,334,335,336,337,338,339,340,341,342,343,344,345,346,3 47,348,349,350,351,352,354,355,356,357,358,359,360,361,362,363,365,366,367,368,37 0,371,373,374,376,377,378,379,380,381} is $(344,5)$ -blocking set as shown in table (15) .by theorem (1) ,there exists a projective $[37,3,32]_{19}$ code which is equivalent to the complete $(37,5)$ -arc k_5

Table (15)

I	$K_5 \cap Li$	$B_{15} \cap Li$
1	287	2,21,40,59,78,97,116,135,173,192,211,230,249,268,306,154,325,3 44,363
2	23	1,21,22,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39
⋮	⋮	⋮
38 0	281,318,36 4	11,31,40,68,96,105,133,142,170,179,207,216,244,253,290,327,355
38 1	185,221	20,22,40,77,95,113,131,149,167,203,239,293,257,275,311,329,347 ,365

4.14 Existence of $[37,3,32]_{19}$ codes

We take 16 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}, C_{13}, C_{14}, C_{15}, C_{16}$ and let

$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12} \cup C_{13} \cup C_{14} \cup C_{15} \cup C_{16}$
 $\{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34 ,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,78,79, 81,94,97,98,101,114,116,117,121,127,135,136,141,143,154,155,161,164,173,174,178,1 81,192,193,201,207,211,212,221,224,230,231,233,241,249,250,261,263,268,269,272,28 1,287,288,289,301,306,307,318,321,325,326,332,341,344,345,353,361,363,364,369,381 \}$.The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 4 points .
- ii. Every point not in K is on at least one 4-secant of K .

The point :

$M = \{40,59,78,97,116,135,154,325,192,211,230,249,268,287,22,24,25,26,27,28,29,30,31, 33,35,36,38,39,3,61,81,101,121,141,161,181,201,301,341,381,321,221,4,5,6,7,8,9,10,12 ,14,16,18,20,11,60,79,117,136,155,174,193,212,250,269,307,345,231,363,289,19,45,13, 37,50,47,51,127,207,48,306,56,32,369,344,178,44,46,49,52,54,56,58,42,43,34,144,164.$ Are eliminated from K to satisfy (1) . The points of index zero for 195,265 are added to K to satisfy (2) , then $K_4 = K \cup [195,265] / M$

$K_4 = \{15,17,23,53,55,57,94,98,143,173,195,224,233,241,261,263,265,272,281,288,318,3 26,332,353,361,364\}$.Is a complete $(26,4)$ –arc as shown in table (16) .Let $\beta_{16} = \pi - k_4 = \{1,2,3,4,5,6,7,8,9,10,11,12,14,16,18,19,20,21,22,24,25,26,27,28,29,30,31,32,33,34,35, 36,37,38,39,40,41,42,43,44,45,46,47,48,49,50,51,52,54,56,58,59,60,61,62,63,64,65,66,6 7,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,89,90,91,92,93,95,96 ,97,99,100,101,102,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,11 8,119,120,121,122,123,124,125,126,127,128,129,130,131,132,133,134,135,136,137,138$

,139,140,141,142,144,145,146,147,148,149,150,151,152,153,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,169,170,171,172,174,175,176,177,178,179,180,181,182,183,184,185,186,187,188,189,190,191,192,193,194,196,197,198,199,200,201,202,203,204,205,206,207,208,209,210,211,212,213,214,215,216,217,218,220,221,222,223,225,226,227,228,229,230,231,232,234,235,236,237,238,239,240,242,243,244,245,246,247,248,249,250,251,252,253,254,255,256,257,258,259,260,262,264,266,267,268,269,270,271,273,274,275,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,294,295,296,297,298,299,300,301,302,303,304,305,306,307,308,309,310,311,312,313,314,315,316,317,319,320,321,322,323,324,325,327,328,329,330,331,333,334,335,336,337,338,339,340,341,342,343,344,345,346,347,348,349,350,351,352,354,355,356,357,358,359,360,362,363,365,366,367,368,370,371,372,373,374,375,376,377,378,379,380,381} is (355,4)-blocking set as shown in table (16) .by theorem (1) ,there exists a projective $[26,3,22]_{19}$ code which is equivalent to the complete (26,4)-arc k_4

Table (16)

I	$K_4 \cap Li$	$B_{16} \cap Li$
1	173	2,21,40,59,78,97,116,135,154,192,211,230,249,268,287,306,325,344,363
2	23	1,21,22,24,25,26,27,28,29,30,31,32,33,35,36,38,39,34,37
⋮	⋮	⋮
38 0	281,318	11,31,40,68,96,105,133,142,170,179,207,216,244,253,290,327,355,364
38 1	∅	20,22,40,77,95,113,131,149,167,185,203,221,239,257,295,275,311,329,347,365

4.17 Existence of $[13,3,10]_{19}$ codes

We take 17 conic, say $C_1, C_2, C_3, C_4, C_5, C_6, C_7, C_8, C_9, C_{10}, C_{11}, C_{12}, C_{13}, C_{14}, C_{15}, C_{16}$ and C_{17} let

$$K = \pi - C_1 \cup C_2 \cup C_3 \cup C_4 \cup C_5 \cup C_6 \cup C_7 \cup C_8 \cup C_9 \cup C_{10} \cup C_{11} \cup C_{12} \cup C_{13} \cup C_{14} \cup C_{15} \cup C_{16} \cup C_{17}$$

{3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,42,43,44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,78,79,81,97,98,101,116,117,121,135,136,141,154,155,161,173,174,181,192,193,201,211,212,221,230,231,241,249,250,261,268,269,281,287,288,301,306,307,321,325,326,341,344,345,361,363,364,381}. The geometrical Structure method must satisfy the following :

- i. K intersects any line of π in at most 3 points .
- ii. Every point not in K is on at least one 3-secant of K .

The point :

$M = \{40,59,78,97,116,135,154,173,192,230,249,268,287,306,325,22,24,25,26,27,28,29,30,31,33,35,36,38,39,3,61,81,101,121,141,161,181,201,301,341,361,381,261,241,4,5,6,7,8,9,10,11,12,13,14,15,16,20,60,79,98,117,136,155,174,212,193,231,250,269,307,345,363,47,17,19,18,173,37,344,32,321,43,44,45,46,48,49,50,23,52,54,56,58,51\}$ Are eliminated from K to satisfy (1) . The points of index zero for 162,202 are added to K to satisfy (2) , then $K_3 = K \cup [162,202] / M$

$K_3 = [34,42,53,55,57,162,202,211,221,281,288,326,364]$. Is a complete (13,3) –arc as shown in table (17) .Let $\beta_{17} = \pi - k_3$

$= \{1,2,3,4,5,6,7,8,9,10,11,12,14,15,16,17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32,33,35,36,37,38,39,40,41,43,44,45,46,47,48,49,50,51,52,54,56,58,59,60,61,62,63,64,65,6$

6,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,89,90,91,92,93,94,95,96,97,98,99,100,101,102,103,104,105,106,107,108,109,110,111,112,113,114,115,116,117,118,119,120,121,122,123,124,125,126,127,128,129,130,131,132,133,134,135,136,137,138,139,140,141,142,143,144,145,146,147,148,149,150,151,152,153,154,155,156,157,158,159,160,161,163,164,165,166,167,168,169,170,171,172,173,174,175,176,177,178,179,180,181,182,183,184,185,186,187,188,189,190,191,192,193,194,196,197,198,199,200,201,203,204,205,206,207,208,209,210,212,213,214,215,216,217,218,220,222,223,224,225,226,227,228,229,230,231,232,233,234,235,236,237,238,239,240,241,242,243,244,245,246,247,248,249,250,251,252,253,254,255,256,257,258,259,260,261,262,263,264,265,266,267,268,269,270,271,273,274,275,276,277,278,279,280,282,283,284,285,286,287,289,290,291,292,293,294,295,296,297,298,299,300,301,302,303,304,305,306,307,308,309,310,311,312,313,314,315,316,317,318,319,320,321,322,323,324,325,327,328,329,330,331,332,333,334,335,336,337,338,339,340,341,342,343,344,345,346,347,348,349,350,351,352,353,354,355,356,357,358,359,360,361,362,363,365,366,367,368,370,371,372,373,374,375,376,377,378,379,380,381} is (368,3)-blocking set as shown in table (17). by theorem (1), there exists a projective $[13,3,10]_{19}$ code which is equivalent to the complete (13,3)-arc k_3

Table (17)

I	$K_3 \cap Li$	$B_{17} \cap Li$
1	211	2,21,40,59,78,97,116,135,154,173,193,230,249,268,287,306,325,344,363
2	\emptyset	1,21,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39
\vdots	\vdots	\vdots
380	281,364	11,31,40,68,96,105,133,142,170,179,207,216,244,253,290,318,327,355
381	\emptyset	20,22,40,77,95,113,131,149,167,185,203,221,239,257,275,293,311,329,347,365

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