

إيجاد الحل المقبول (الممكن) والأمثل لأنموذج البرمجة الخطية في ظل عدم تحقق شرطيّ الإمكانية والأمثلية

1- الخلاصة

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Abstract

Consider the Linear Programming (LP) active & effective factor in decision maker & taker process . So that given certain goals , the Significance of (LP) in solving & evaluation the activity during one tools (General Simplex Mehtod)that the solution is Feasible &no optimal then called (Primal Simplex Method) or vice-versa then called(Dual Simplex Method).Same of cases the solution is infeasible & no optimal then using the two methods alternatively once to find the feasible solution and other to find optimal solution

2- المقدمة

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(1950)

3- الجانب النظري

(6)(7)(8)(9)(10)

1-3



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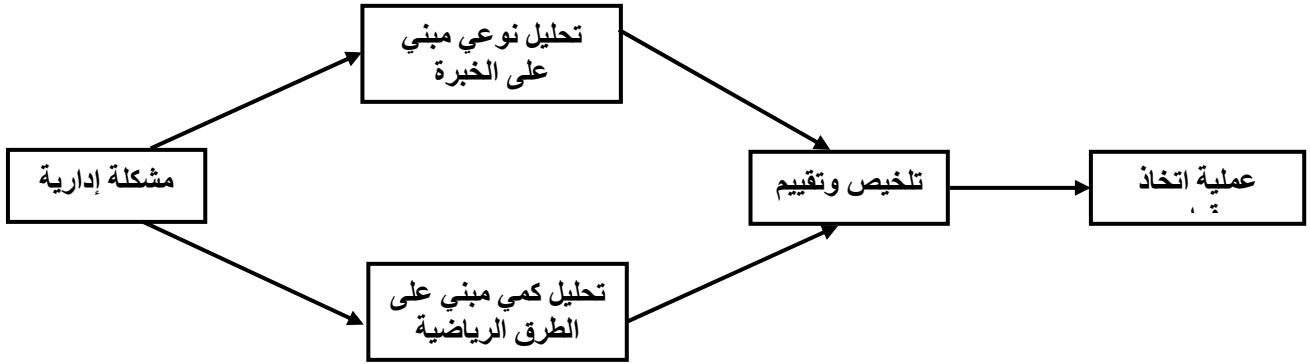


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2-3

(1-2-3)



(1-2-3)

(1-2-3)

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() 3-3

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- (Max) _____ -1
- (Min) _____ -2
- :() _____
-
- : _____ -3

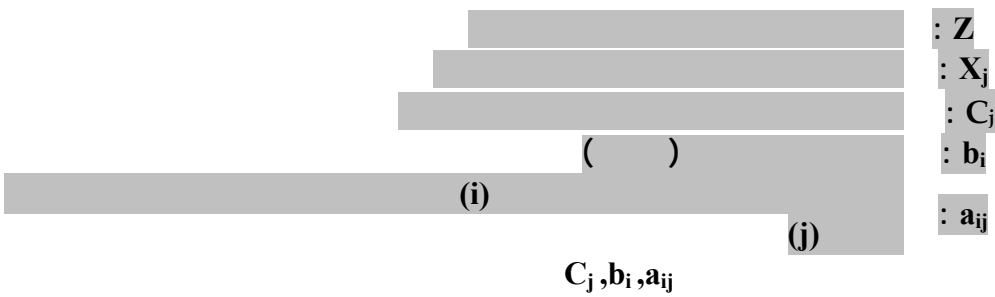
Max or Min

$$Z = \sum_{j=1}^{j=n} C_j X_j$$

S.T.

$$\sum_{j=1}^{j=n} a_{ij} X_j (\leq, =, \geq) b_i ; i = 1, 2, \dots, m$$

$$X_j \geq 0 ; j = 1, 2, \dots, n$$



1-3-3

<p>Max</p> $Z = \sum_{j=1}^{j=n} C_j X_j$ <p>S.T.</p> $\sum_{j=1}^{j=n} a_{ij} X_j \leq b_i \quad ; i = 1, 2, \dots, m$ $X_j \geq 0 \quad ; j = 1, 2, \dots, n$

(Max)



1-3-3

<p>Max or Min</p> $Z = \sum_{j=1}^{j=n} C_j X_j$ <p>S.T.</p> $\sum_{j=1}^{j=n} a_{ij} X_j \mp S_i = b_i \quad ; i = 1, 2, \dots, m$ $X_j, S_i \geq 0 \quad ; j = 1, 2, \dots, n$
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(+) : +S_i

(-) : -S_i

(Min) (Max) ❖
() ❖
❖
❖

4-3

(General Simplex Method)

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1947 (George Dantzing)

(Primal – Simplex Method) 1-4-3

(Dual – Simplex Method) 2-4-3

(Big M – Simplex Method) 3-3-4

(Two Phase – Simplex Method) 4-4-3

(2-4-3) (1-4-3)

(Primal – Simplex Method) 1-4-3

()

(Feasible & No Optimal)

:
() -1
(Z – Row)

(Starting Basic Feasible Solution)

-2

C _B	B.V.	C ₁	C ₂	C _n	0	0	0	Rhs
		X ₁	X ₂	X _n	S ₁	S ₂	S _m	
0	S ₁	a ₁₁	a ₁₂	a _{1n}	1	0	0	b ₁
0	S ₂	a ₂₁	a ₂₂	a _{2n}	0	1	0	b ₂
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
0	S _m	a _{m1}	a _{m2}	a _{mn}	0	0	1	b _m
Z - Row		±C ₁	±C ₂	±C _n	0	0	0	0

Max - C
+ C

Min

: -3

(Optimality Condition)

(Non - Basic Entering Variable)

()

(Min)

(Max)

.()

()

(Feasibility Condition)

(Basic Leaving Variable)

Min Max
(Feasible Area) ♦

(Updating the Solution)

-4

()

(Gauss Method)

$$\begin{aligned}
 & \div (\quad) = \quad - \\
 & * (\quad) - (\quad) = \quad - \\
 & (\quad)
 \end{aligned}$$

Stopping Stage -5

()

Max

-

Min

-

(Dual – Simplex Method)

2-4-3

()

(Optimal & Infeasible)

$$\begin{aligned}
 & (\quad) \quad -1 \\
 & (Z - Row) \quad (\quad)
 \end{aligned}$$

(Starting Optimal Infeasible

-2

Solution)

C _B	B.V.	C ₁	C ₂	C _n	0	0	0	Rhs
		X ₁	X ₂	X _n	S ₁	S ₂	S _m	
0	S ₁	a ₁₁	a ₁₂	a _{1n}	1	0	0	±b ₁
0	S ₂	a ₂₁	a ₂₂	a _{2n}	0	1	0	±b ₂
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
0	S _m	a _{m1}	a _{m2}	a _{mn}	0	0	1	±b _m
Z - Row		±C ₁	±C ₂	±C _n	0	0	0	0

Max +C

Min - C



	:	-3
(Feasibility Condition)	:	
(Basic Leaving Variable)		
()		
	Min	Max
(Optimality Condition)	:	
(Non – Basic Entering Variable)		
()		
(Max)	(Min)	
(Updating the Solution)		-4
	(Gauss Method)	
	Stopping Stage	-5
	Min	Max
Max		
(1-4-3)		
		(2-4-3)

() -4

: _____
()

Max Min

() : _____

:(1)

Min

$$Z = 2X_1 - 3X_2 + X_3$$

S.T.

$$5X_1 + 2X_2 - X_3 = 10$$

$$X_1 - 4X_2 + 3X_3 \leq 12$$

$$X_j \geq 0 ; j = 1,2,3$$

: _____

Min

$$Z = 2X_1 - 3X_2 + X_3$$

S.T.

$$5X_1 + 2X_2 - X_3 \leq 10$$

$$5X_1 + 2X_2 - X_3 \geq 10$$

$$X_1 - 4X_2 + 3X_3 \leq 12$$

$$X_j \geq 0 ; j = 1,2,3$$

: _____

(1-)

Min

$$Z = 2X_1 - 3X_2 + X_3$$

S.T.

$$5X_1 + 2X_2 - X_3 \leq 10$$

$$-5X_1 - 2X_2 + X_3 \leq -10$$

$$X_1 - 4X_2 + 3X_3 \leq 12$$

$$X_j \geq 0 ; j = 1,2,3$$

() : _____

Min

$$Z - 2X_1 + 3X_2 - X_3 = 00$$

S.T.

$$5X_1 + 2X_2 - X_3 + S_1 = 10$$

$$-5X_1 - 2X_2 + X_3 + S_2 = -10$$

$$X_1 - 4X_2 + 3X_3 + S_3 = 12$$

$$X_j \geq 0 ; S_i \geq 0 ; i, j = 1,2,3$$

: _____

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	5	2	-1	1	0	0	10
0	S ₂	-5	-2	1	0	1	0	-10
0	S ₃	1	-4	3	0	0	1	12
Z - Row		-2	3	-1	0	0	0	0
Ratio	Z / S ₂	2/5	3/2	

C _B	B.V.	S ₂		X ₁		0	0	RHS
		2	-3	1	0			
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
2	X ₁	1	2/5	-1/5	0	-1/5	0	2
0	S ₃	0	-2/5	16/5	0	1/5	1	10
Z - Row		0	19/5	-7/5	0	2/5	0	4

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C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
2	X ₁	1	2/5	-1/5	0	-1/5	0	2
0	S ₃	0	-2/5	16/5	0	1/5	1	10
Z - Row		0	19/5	-7/5	0	2/5	0	4

X₁ X₂

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
-3	X ₂	5/2	1	-1/2	0	-1/2	0	5
0	S ₃	1	0	3	0	0	1	12
Z - Row		-19/2	0	1/2	0	3/2	0	-15

S₁ S₂

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₂	0	0	0	1	1	0	0
-3	X ₂	5/2	1	-1/2	1/2	0	0	5
0	S ₃	1	0	3	0	0	1	12
Z - Row		-19/2	0	1/2	-3/2	0	0	-15

S₃ X₃

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₂	0	0	0	1	1	0	0
-3	X ₂	8/3	1	0	1/2	0	1/6	7
1	X ₃	1/3	0	1	0	0	1/3	4
Z - Row		-29/3	0	0	-3/2	0	-1/6	-17

Max

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
2	X ₁	1	2/5	-1/5	0	-1/5	0	2
0	S ₃	0	-2/5	16/5	0	1/5	1	10
Z - Row		0	19/5	-7/5	0	2/5	0	4

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
2	X ₁	1	2/5	-1/5	0	-1/5	0	2
0	S ₃	0	-2/5	16/5	0	1/5	1	10
Z - Row		0	19/5	-7/5	0	2/5	0	4

S₃ X₃

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	0	0	0	1	1	0	0
2	X ₁	1	3/8	0	0	-3/16	1/16	21/40
1	X ₃	0	-1/8	1	0	1/16	5/16	25/8
Z - Row		0	29/8	0	0	-5/16	7/16	167/40

S₁ S₂

C _B	B.V.	2	-3	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₂	0	0	0	1	1	0	0
2	X ₁	1	3/8	0	3/16	0	1/16	21/40
1	X ₃	0	-1/8	1	-1/16	0	5/16	25/8
Z - Row		0	29/8	0	5/16	0	7/16	167/40

:(2)

Max

$$Z = 2X_1 - X_2 + X_3$$

S.T.

$$2X_1 + 4X_2 + 5X_3 \geq 15$$

$$X_1 + 9X_2 + 2X_3 \geq 03$$

$$4X_1 + 6X_2 + 2X_3 \leq 08$$

$$X_j \geq 0 ; j = 1,2,3$$

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
0	S ₁	-2	-4	-5	1	0	0	-15
0	S ₂	-1	-9	-2	0	1	0	-3
0	S ₃	4	6	2	0	0	1	8
Z - Row		-2	1	-1	0	0	0	0
Ratio	Z / S₁	1	1/4	1/5	

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	2/5	4/5	1	1/5	0	0	3
0	S ₂	-1/5	-37/5	0	2/5	1	0	3
0	S ₃	16/5	22/5	0	-2/5	0	1	2
Z - Row		-8/5	9/5	0	-1/5	0	0	3

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	2/5	4/5	1	1/5	0	0	3
0	S ₂	-1/5	-37/5	0	2/5	1	0	3
0	S ₃	16/5	22/5	0	-2/5	0	1	2
Z - Row		-8/5	9/5	0	-1/5	0	0	3

S₃ X₁

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	0	1/4	1	3/20	0	-1/8	11/4
0	S ₂	0	57/8	0	17/40	1	1/16	25/8
2	X ₁	1	11/8	0	1/8	0	5/16	5/8
Z - Row		0	4	0	17/5	0	1/2	4

Min

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	2/5	4/5	1	1/5	0	0	3
0	S ₂	-1/5	-37/5	0	2/5	1	0	3
0	S ₃	16/5	22/5	0	-2/5	0	1	2
Z - Row		-8/5	9/5	0	-1/5	0	0	3

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	2/5	4/5	1	1/5	0	0	3
0	S ₂	-1/5	-37/5	0	2/5	1	0	3
0	S ₃	16/5	22/5	0	-2/5	0	1	2
Z - Row		-8/5	9/5	0	-1/5	0	0	3

S₃ X₂

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	2/11	0	1	7/55	0	-2/11	29/11
0	S ₂	57/11	0	0	59/55	1	37/11	70/11
-1	X ₂	8/11	1	0	1/11	0	5/22	5/11
Z - Row		-28/11	0	0	2/55	0	-9/22	24/11

X₂ X₄

C _B	B.V.	2	-1	1	0	0	0	RHS
		X ₁	X ₂	X ₃	S ₁	S ₂	S ₃	
1	X ₃	-46/55	-7/5	1	0	0	-1/2	2
0	S ₂	-17/5	-59/5	0	0	1	-1	1
0	S ₁	8	11	0	1	0	5/2	5
Z - Row		-156/55	-2/5	0	0	0	-1/2	2

5- الاستنتاجات

.Min

Max

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() :

() :

6- المصادر

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