

# التحليل الاحصائي لتجارب القياسات المكررة للبيانات المصنفة في حالة معالجتين وثلاث معالجات

المستخلص

Subject ( )

(Categorical Count Data)

Cochran, Mc Nemar, Ireland & Kullback, Stuart, Bhapkar, )

( ) (Ireland & Ku & Kullback

(Stuart, Bahapkar, Ireland & Ku & Kullback)

( )

WLS

(Cochran, Ireland & Kullback,)



**المقدمة والهدف**

(Subjects)

**"Categorical or Count Data"**

(18)(Mc-Nemar) 1949  
 Two-Way ( )  
 (7)(Cochran) 1950  
 C r Two-Way ( )  
 (19)(Stuart) 1955  
 (Marginal Probabilities)  
 1966 ( - )  
 (4)(Bhapkar)  
 1968 .r×r  
 (11)(KullBack & Ireland)  
 2×2  
 (13)(Ireland) 1969 .2×2×2  
 (9)(Crizzle) .r×r  
 i=1,...,s, ni  
 (15)(KullBack) 1971 . r  
 .( ) r×r×r×r×...



(14)(CARY G. Koch)

1977

$\chi^2$

B's

(3)(Agresti & Pendergast)

1986

(6)(Park & Davis)

1993

1969

Stramer & Koch Grizzle

(18)(Sheskin, D.J.)

2001

( )

( )

2005

(2)(Lius Agresti)  
(Ordinal)

(Subject)

**الجانب النظري**

r

:

( )

( )

:

:

:(18)(7) Cochran Q -1

n

(Dichotomous)

(Two Mutually Exclusive Categories)

( )

(Subjects)

:

(1)

$H_0 : \pi_1 = \pi_2$

$j^{th}$

$\pi$

. Response

$\pi_j$

: Cochran

$$Q = \frac{(k-1)[(k)(c) - (T^2)]}{(k)(T) - R}$$

(2)



$$T = \sum R_i$$

$$R = \sum R_i^2$$

nk < 24

n < 4

Patil (1975)

Cochran Test

n > 4, nk > 24

Mc Nemar <sup>(18)</sup> - 2

Mc Nemar (Subject) Pretest Posttest  
 Cochran Q (Before-After Design) (Dichotomous)

Mc Nemar (1) (1)

/				
		a	b	a+b=n <sub>1</sub>
		c	d	c+d=n <sub>2</sub>
		a+c	b+d	N

a,b,c,d

(unit)

$H_0 : \pi_b = \pi_c$  (3)

$\chi^2 = \frac{(b-c)^2}{b+c}$  (4)

.df=1



**:(12) Ireland & KullBack -3**

(12) Ireland & KullBack

(

$P_{ij}$   $2 \times 2$

$\hat{P}_{i.}, \hat{P}_{.j}$  (Marginal Probabilities)

[BAN]

(Principle of Minimum Discrimination information)

(Best Asymptotically Normal)

(12)

(Convergent Iterative Procedure)

: (Ireland and Kull Back)

$$\sum_i \sum_j \pi_{ij} = 1 \quad \pi_{ij} > 0 \quad i=1, \dots, r, j=1, \dots, c \quad \{\pi_{ij}\}$$

$$P_{.j} = \sum_i P_{ij}, \quad P_{i.} = \sum_j P_{ij} \quad \{P_{ij}\}$$

$\pi_{ij}$

$P_{ij}$

(Measure)

Distance

.(Discrimination Information)

$$I(P : \pi) = \sum_i \sum_j P_{ij} \ln \frac{P_{ij}}{\pi_{ij}} \quad (5)$$

$P_{ij}$

$I(P : \pi)$

$P_{ij}^*$

$.P^*$

:

Iterations

$$\left. \begin{aligned} P_{ij}^{(2n-1)} &= \frac{P_{i.}}{P_{i.}^{(2n-2)}} P_{ij}^{(2n-2)} \\ P_{ij}^{(2n)} &= \frac{P_{.j}}{P_{.j}^{(2n-1)}} P_{ij}^{(2n-1)} \\ P_{ij}^{(\circ)} &= \pi_{ij} \end{aligned} \right\}$$

(6)

$$\hat{P}_{ij} = n_{ij} / n : \pi_{ij}$$

:

$$\sum_i \sum_j n_{ij} = n$$

$ij^{th}$

$:n_{ij}$

: (MDI)

BAN

:  $P_{ij}^*$  .Minimize Set

$$2nI(\hat{P}^* : \hat{P}) = 2n \sum_i \sum_j \hat{P}_{ij}^* \ln(\hat{P}_{ij}^* / \hat{P}_{ij}) \quad (7)$$



(Marginal homogeneity)

$$P_{(i)} = P_{(i)} \quad \sum_{i=1}^r P_{(i)} = 1,$$

$$\chi^2 \quad (MDI) \quad \chi^2$$

Stuart -1 (19)

Stuart (Subjects) (Unit) (Categorical) (Two-Ways) [ n ]

$$H_0 : P_{i.} = P_{.i} \quad (8)$$

$$P_{i.} = \sum_j P_{ij}$$

$$P_{.j} = \sum_i P_{ij}$$

$$\sum_i \sum_j P_{ij} = \sum_i P_{i.} = \sum_j P_{.j} = 1$$

$$Q = \sum_{i,j=1}^{r-1} V^{ij} d_i d_j \quad (9)$$

$$Q = \sum_{i,j} a_{ij} d_i d_j \quad H_0 \quad \sum d_i = 0 \quad (r-1)$$

(redundant variate)

$$Q = \sum_{i,j=1}^{r-1} V^{ij} d_i d_j$$

Loglikelihood

(19)



$$\left. \begin{aligned} V_{ii} &= n_{i.} + n_{.i} - 2n_{ii} \\ V_{ij} &= -(n_{ij} + n_{ji}) \end{aligned} \right\} \quad (10)$$

(11)

$i, j = 1, 2, \dots, r-1$

$V_{ij}$

(10)

Q

$V_{ij}$

:  $V_{ii}$   
:  $V_{ij}$

(9)

Q

$d_i = n_{i.} - n_{.i}$

-1  
-2  
-3  
-4

V

(10)

$\chi^2$

Q

$H_0$

(r-1)

:<sup>(4)</sup>BHAPKAR

(2)

BHAPKAR

$P_{ij}$

$r \times r$

:  $i^{\text{th}}$   $j^{\text{th}}$

$I, J = 1, \dots, r$   
 $\sum_{ij} P_{i,j} = 1$

(8)

r-1

$H_0$

$$F_{k(P)} \equiv P_{k.} = P_{.k} = 0$$

$I, J = 1, \dots, r$

$k = 1, 2, \dots, r-1$   
 $= n_{ij}$

$$N = \sum_{ij} n_{ij}$$

: BHAPKAR

$$\chi_j^2 = d'w^{-1}d$$

(12)

$$d = n_{k.} - n_{.k}$$

(13)

:

) w

:Bhapkar

:

w

(d (r-1)k )

$$w = [\delta_{kk'}(n_{k.} + n_{.k'}) - n_{kk'} - n_{k'k} - N^{-1}d_k d_{k'}]$$

(14)

$$\delta_{kk'} = 1 \quad \text{if } k = k'$$

$$0 \quad \text{other wise}$$

(r-1)

$\chi^2$

$\chi_j^2$

(r-1)

$\chi^2$

$\chi_j^2$



**:(12) Ireland & Ku & Kull Back -3**

**(12) Ireland & Ku & KullBack**

( )

$r \times r$

$P_{.j}, P_{.i}$

$P_{ij}$

(3- )

**(Minimum Discrimination Information)**

**(Convergent Iterative Procedure)**

$i^{th}$

$$n_{(ij)} \quad \pi_{(ij)} = \frac{n_{.j}}{n}$$

**I(P:  $\pi$ )**

$$P_{(ij)} \quad \sum \sum n_{(ij)} = n \quad jth$$

(5)

$$P_{(i)} = \sum_j P_{(ij)} = P_{(j)} = \sum_k P_{(ki)}$$

:

$$P_{(ij)}^{(n+1)} = \left[ \frac{P_{(i)}^{(n)} P_{(j)}^{(n)}}{P_{(i)}^{(n)} P_{(j)}^{(n)}} \right]^{1/2} P_{(ij)}^{(n)} C_n \quad (15)$$

:

$$C_n = 1 / \sum \sum \left[ \frac{P_{(i)}^{(n)} P_{(j)}^{(n)}}{P_{(i)}^{(n)} P_{(j)}^{(n)}} \right]^{1/2} P_{(ij)}^{(n)} \quad (16)$$

$$P_{(ij)}^o = \pi_{(ij)}$$

:

: (MDI)

$$2n \ln(P^* : \pi) = 2n \sum \sum P_{(ij)} \ln \frac{P_{(ij)}^*}{\pi_{(ij)}} \quad (17)$$

(r-1)  $\chi^2$

$\cdot \chi^2$  (M.D.I)

:

( )  
( )

( )





(18) **Cochran** <sup>(7)</sup> <sup>(18)</sup> -1

(2) Q (1- )

$$H_0 : \pi_1 = \pi_2 = \pi_3 \tag{18}$$

(15) **Ireland & KullBack** -2

(3- ) (Iterative Procedure)  $2 \times 2 \times 2$

$$H_1 : \text{Not } H_0$$

$k=1, \dots, t, \quad j=1, \dots, s, \quad i=1, \dots, r \quad \{\pi_{ijk}\}$

$\sum_i \sum_j \sum_k \pi_{ijk} = 1 \quad \pi_{ijk} > 0$

$$I(P : \pi) = \sum_i \sum_j \sum_k P_{ijk} \ln \frac{P_{ijk}}{\pi_{ijk}} \tag{19}$$

$P_{ijk}^*$

(Iterations)

$$\left. \begin{aligned} P_{ijk}^{(3n+1)} &= \frac{P_{i..}}{P_{i..}^{(3n)}} P_{ijk}^{(3n)} \\ P_{ijk}^{(3n+2)} &= \frac{P_{.j.}}{P_{.j.}^{(3n+1)}} P_{ijk}^{(3n+1)} \\ P_{ijk}^{(3n+3)} &= \frac{P_{..k}}{P_{..k}^{(3n+2)}} P_{ijk}^{(3n+2)} \end{aligned} \right\} \tag{20}$$

$$P_{ijk}^{(0)} = \pi_{ijk} \quad , n = 1, 2, \dots$$



(ijk-th)  $n_{ijk}$   $\hat{P}_{ijk} = \frac{n_{ijk}}{n}$   $\pi_{ijk}$

$\hat{P}_{ijk}^*$  (Minimizing Set)  $(\sum \sum \sum n_{ijk} = n)$

: (MDI) BAN

$$2nI(\hat{P}^* : \hat{P}) = 2n \sum_i \sum_j \sum_k \hat{P}_{ijk}^* \ln(\hat{P}_{ijk}^* / \hat{P}_{ijk}) \quad (21)$$

(r+s+t-3)  $\chi^2$

: (Marginal Homogeneity)  $r = s = t$

$P_{(i..)} = P_{(.i.)} = P_{(..i)}$ ,  $i=1, \dots, r$

$\sum P_{i..} = 1$

$\chi^2$  (MDI)  $(r+s+t-3)$

: (5) -3

(WLS) *Weighted Least Square-WLS-*

(Units)

d

$r = L^d$

: (Response Profile) :r

:d

:L

(Response Profile)  $r=L^d$   $i=1, \dots, r$

$i= 1, \dots, s$ ,  $n_i$  (Sub Population) d

$n_{ij}$  (5)  $s \times r$

$i^{th}$  j

(5)

( )						Total
	1	2	...	r	...	
1	$n_{11}$	$n_{12}$	...	$n_{1r}$	...	$n_{1.}$
2	$n_{21}$	$n_{22}$	...	$n_{2r}$	...	$n_{2.}$
:	:	:	...	:	...	:
s	$n_{s1}$	$n_{s2}$	...	$n_{sr}$	...	$n_{s.}$



$$.P_{ij} = n_{ij} / n_i \quad P_{ij}$$

$$P'_i = [P_{i1}, P_{i2}, \dots, P_{ir}]$$

$$P' = [P'_1, P'_2, \dots, P'_s]$$

. P

(Consistent Estimator)

$$v_{(P_i)} = \frac{1}{n_i} [DP_i - P_i P'_i] \quad , i=1,2,\dots,s \quad (22)$$

$$v(P_i) = \frac{1}{n_i} \begin{bmatrix} P_{i1}(1-P_{i1}) & -P_{i1}P_{i2} & \dots & -P_{i1}P_{ir} \\ -P_{i1}P_{i2} & P_{i2}(1-P_{i2}) & \dots & -P_{i2}P_{ir} \\ \vdots & \vdots & \ddots & \vdots \\ -P_{i1}P_{ir} & -P_{i2}P_{ir} & \dots & P_{ir}(1-P_{ir}) \end{bmatrix}$$

$$F' = F'(p) = [F_1(p), \dots, F_u(p)]$$

: F(p)

$$F(p) \sim Nu(F(\pi), V_F)$$

: F : V\_F

$$V_F = Av(p)A'$$

(23)

p F

$$A = [dF(x) / dx / x = p]$$

.F(π) F (u×sr)

F(p)

$$\underline{F}(\pi) = A \underline{\pi}$$

u≤s(r - t) :A

$$V_F \quad . \underline{\pi}$$

(WLS)

$$\underline{F}(\pi) = X \underline{\beta} \quad (24)$$

:

$$W = (F - Xb)' V_F^{-1} (F - Xb) \quad (25)$$





:Cochran

(2)

(1- )

Cochran

:

(1)

(2)

(1)

 $R_i$  (0)

No.	(ARB)	(ACE-1)	$R_i$	$R_i^2$
1	1	1	2	4
2	0	1	1	1
3	0	1	1	1
4	1	1	2	4
5	1	1	2	4
6	1	1	2	4
7	0	0	0	0
8	1	0	1	1
9	1	0	1	1
10	1	1	2	4
11	1	1	2	4
12	0	1	1	1
13	0	0	0	0
14	1	0	1	1
15	0	0	0	0
16	1	0	1	1
17	0	1	1	1
18	1	1	2	4
19	1	1	2	4
20	1	1	2	4
21	0	1	1	1
22	1	0	1	1
23	0	1	1	1
24	0	0	0	0
25	0	0	0	0
26	1	1	2	4
27	0	0	0	0
28	1	1	2	4
29	1	1	2	4
30	1	0	1	1
31	1	1	2	4
32	0	1	1	1
33	1	1	2	4
34	0	0	0	0
35	1	0	1	1
36	1	1	2	4
37	1	1	2	4
38	0	1	1	1
39	0	0	0	0
40	0	1	1	1
41	1	1	2	4
42	1	1	2	4
43	1	0	1	1
44	0	0	0	0
45	0	1	1	1
46	1	1	2	4
47	1	1	2	4
48	0	1	1	1
49	1	1	2	4



50	0	0	0	0
51	1	0	1	1
52	1	1	2	4
53	0	1	1	1
54	0	0	0	0
55	1	1	2	4
56	1	1	2	4
57	1	0	1	1
58	1	1	2	4
59	0	1	1	1
60	1	1	2	4
61	1	1	2	4
62	1	1	2	4
63	0	1	1	1
64	1	1	2	4
65	1	1	2	4
66	1	0	1	1
67	0	0	0	0
68	1	0	1	1
69	1	1	2	4
70	1	1	2	4
71	1	1	2	4
72	1	0	1	1
73	0	0	0	0
74	1	1	2	4
75	1	0	1	1
76	1	1	2	4
77	1	1	2	4
78	0	1	1	1
79	0	0	0	0
80	1	1	2	4
81	1	1	2	4
82	0	1	1	1
83	1	1	2	4
84	1	1	2	4
85	1	1	2	4
86	1	1	2	4
87	0	1	1	1
88	1	1	2	4
89	1	1	2	4
90	1	1	2	4
91	0	0	0	0
92	1	1	2	4
	$\sum C_1 = 60$	$\sum C_2 = 63$	123	215



$$\chi^2_{(1)} = 6.63, \chi^2_{(0.05)} = 3.84$$

**Mc Nemar**

$$\chi^2_{(2)} = 0.290, \chi^2_{(0.05)} = 3.89, \chi^2_{(0.01)} = 6.63$$

2x2 (3)

/ARB				
ACF-I		15	14	29
		17	46	63
		32	60	92

**Ireland & KullBack**

Ireland & KullBack (3) (Cycles) 3 (3)

1			
2	0.1391	0.1608	0.2999
	0.1609	0.539	0.6999
	0.3	0.6998	0.9998

1			
2	0.1391	0.1608	0.2999
	0.1608	0.5391	0.6999
	0.2999	0.6999	0.9998

(MDI)  $2nI(\hat{P}^* : P) = 0.9218$

0.9218

(2)  $\chi^2_{(0.01)} = 9.21, \chi^2_{(0.05)} = 5.991$



**:Stuart**

(3) (1- ) Stuart  
 (9) (d<sub>2</sub>) V (8)  
 Q Q = 0.29 (9) d<sub>1</sub> Q = 0.29  
 $\chi^2_{0.01} = 6.63$   $\chi^2_{0.05} = 3.841$  (1)  $\chi^2$  Q

**:Bhapkar**

(2 - ) bhapkar  
 $\chi^2_j = 0.29$  (12) (8) (3)  
 $\chi^2_{0.01} = 6.63$   $\chi^2_{0.05} = 3.891$  (1)  $\chi^2$   
 $\chi^2_j$   $\chi^2$

**:Ireland & Ku & KullBack**

Ireland & Ku & (3) KullBack  
 (15) (3- ) :

1 \ 2			
	46.06	15.81	61.87
	15.09	15.02	30.11
	61.15	30.83	91.98

1 \ 2			
	46.07	15.53	61.6
	15.36	15.02	30.38
	61.43	30.55	91.98

$\chi^2$  0.21 (MDI)  
 ( )  
 (MDI)  $\chi^2_{0.01} = 3.63$   $\chi^2_{0.05} = 3.891$  (1)  
 $\chi^2_{0.05}$   
 ( )





**بيانات القياسات المكررة للبيانات المصنفة في حالة معالجتين وكل  
معالجة باكثر من مستويين:**

(2004 - 2001)

( )  
100 400  
( )  
: Stuart  
Stuart (8)  
(4) 4x4 (1- )  
Q = 0.8552 (9) V  
 $\chi^2_{(4-1)}$  Q Q = 0.7221 (9)  
Q  $\chi^2_{0.01} = 7.815$  ,  $\chi^2_{0.05} = 11.34$  3  $\chi^2$   
 $\chi^2$

400 4x4 (4)

	81	14	7	4	106
	13	80	23	5	121
	6	19	94	11	130
	2	5	10	26	43
	102	118	134	46	400

**:Bahapkar**  
(4) (2- ) Bahapkar (9)  
 $\chi^2_j = 0.8576$  (13)  
(3)  $\chi^2$   
 $\chi^2$   $\chi^2_j$   $\chi^2_{0.05} = 11.34$   $\therefore \chi^2_{0.01} = 7.82$





**:Cochran**

(1- ) Cochran (18)

$$Q = \frac{\chi^2}{\chi^2_{0.05} = 9.215, \chi^2_{0.01} = 5.991} \quad (2)$$

$\chi^2$

**:Ireland & KullBack**

Ireland & KullBack (20) 13 (2- )

$X_{(ijk)}$

i	J		0		$X_{(i..)}$
	K	1	1	0	
1	168.75	23.43	27.18	20.62	239.98
0	25.55	21.11	11.11	102.22	159.99
	194.3	44.54	38.29	122.84	399.97

$X_{(j..)} = 238.84 \quad 161.13$   
 $X_{(..k)} = 232.59 \quad 167.38$

i	J		0		$X_{(i..)}$
	K	1	1	0	
1	171.57	20.91	28.35	18.91	239.74
0	27.58	20.04	12.28	99.91	159.81
	199.15	40.95	40.63	118.82	399.55

159.45  $X_{(j..)} = 240.1$   
 159.77  $X_{(..k)} = 239.78$

:  
 $X_{(ijk)}$   
 :j  
 :i  
 :k  
 :0  
 :1

**2.37 (MDI)**

$$\chi^2_{0.05} = 11.34 \quad \chi^2_{0.01} = 7.85 \quad (3) \quad \chi^2$$

$\chi^2$  (MDI)



:

Weighted least square (WLS)

(3- ) (26)

$r=L^d=2^3=8$

$d=3$

( )

$L=2$

$(S=1)$

(Response Profiles)

: (WLS)

(6)

S	S	S	S	F	F	F	F	
S	S	F	F	S	S	F	F	
S	F	S	F	S	F	S	F	
180	25	29	22	23	19	10	92	400

.Failer

:F

.Successes

: S

:

$\underline{P} = (0.45, 0.0625, 0.0725, 0.055, 0.0575, 0.0475, 0.025, 0.23)'$   
 $i^{th}$

:  $F_{(P)} = (P_1, P_2, P_3)'$

:P<sub>2</sub>

:P<sub>1</sub>

:P<sub>3</sub>

.Marginal Proportions

.Linear Transformation

$F_{(P)} = AP$

$A = \begin{pmatrix} 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 \end{pmatrix}$

:

:

$F_{(P)} = \begin{pmatrix} 0.64 \\ 0.618 \\ 0.605 \end{pmatrix}$

:

$X = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, C = \begin{pmatrix} 1 & -1 & 0 \\ 1 & 0 & -1 \end{pmatrix}$



$$: \quad (22) \quad V_{(P)}$$

$$1.0e-003^*$$

$$V_{(P)} = \begin{bmatrix} 0.6188 & -0.0703 & -0.0816 & -0.0619 & -0.0647 & -0.0534 & -0.0281 & -0.2588 \\ -0.0703 & 0.1465 & -0.0113 & -0.0086 & -0.0090 & -0.0074 & -0.0039 & -0.0359 \\ -0.0816 & -0.0113 & 0.1681 & -0.0100 & -0.0104 & -0.0086 & -0.0045 & -0.0417 \\ -0.0619 & -0.0086 & -0.0100 & 0.1299 & -0.0079 & -0.0065 & -0.0034 & -0.0316 \\ -0.0647 & -0.0090 & -0.0104 & -0.0079 & 0.1355 & -0.0068 & -0.0036 & -0.0331 \\ -0.0534 & -0.0074 & -0.0086 & -0.0065 & -0.0068 & 0.1131 & -0.0030 & -0.0273 \\ -0.0281 & -0.0039 & -0.0045 & -0.0034 & -0.0036 & -0.0030 & 0.0609 & -0.0144 \\ -0.2588 & -0.0359 & -0.0417 & -0.0316 & -0.0331 & -0.0273 & -0.0144 & 0.4427 \end{bmatrix}$$

$$: \quad (23) \quad V_F$$

$$1.0e-003^*$$

$$V_F = \begin{pmatrix} 0.5760 & 0.2933 & 0.3383 \\ 0.2933 & 0.5905 & 0.3348 \\ 0.3383 & 0.3348 & 0.5974 \end{pmatrix}$$

$$:(2-42) \quad (b)$$

$$b = \begin{pmatrix} 0.6400 \\ 0.6175 \\ 0.6050 \end{pmatrix}$$

$$(0) \quad (2-39) \quad (2-38)$$

$$W_c = (0.8542) \quad (2-41)$$

$$W_c \quad \chi_{0.05}^2 = 9.215 \quad \chi_{0.01}^2 = 5.991 \quad (2) \quad \chi^2 \quad W_c$$

$$\chi^2$$



## الاستنتاجات

-1

Bhapkar Stuart McNemar Cochran

McNemar Cochran

Cochran

McNemar

Bhapkar Stuart

V W

d

N

(MDI)

Ireland &amp; KullBack

Ireland &amp; KullBack

Bhapkar Stuart

-2

Stuart

(4)

Bhapkar

Ireland &amp; Ku &amp;

KullBack

WLS

Ireland &amp; Ku &amp; Kullback Cochran

-3

)

.(  
(WLS)

-4

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## التوصيات

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